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

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ABSTRACT

Reconfigurable coupled-resonator elastic waveguides are formed using defects composed of threaded rods, fixed with nuts and attached to a perforated two-dimensional phononic crystal slab. The resonant frequency of the defect can be tuned continuously within a complete phononic bandgap by adjusting the length of the threaded rod. Straight waveguides are formed from a line of defects. Phononic circuits are created by coupling three parallel straight waveguides. Through precise manipulation of the length of the threaded rod assembly, frequency demultiplexing of Lamb waves is achieved. Numerical and experimental results are found to be in good agreement. This work is of significance for the practical design of phononic devices including reconfigurable circuits.

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The study of modulating elastic waves in artificial periodic structures has attracted a lot of attention.^{1,2} Phononic crystals (PCs),^{3,4} as a functional composite material with spatial periodicity, are characterized by bandgap.^{5,6} In the frequency range where the bandgap is located, the propagation of elastic/acoustic waves is forbidden, and only evanescent waves with spatial attenuation are allowed,⁷ which gives phononic crystals applications in vibration isolation,⁸ filtering,⁹ and so on. The introduction of defects breaks the original periodicity, and defect states can arise inside bandgaps. As a result, waves can propagate along a linear chain of defect cavities.¹⁰ Innovative elastic wave devices can be designed, e.g., waveguides,¹¹ splitters,¹² multiplexers, and demultiplexers.^{13,14}

Recently, the propagation of Lamb waves in defect chains^{15–17} has been increasingly studied. Based on linear waveguides, the concept of coupled-resonator optical waveguides (CROWs)¹⁸ was first introduced in the field of photonics. Subsequently, the concepts of coupled-resonator elastic waveguides (CREWs)¹⁶ and coupled-resonator acoustic waveguides (CRAWs) inspired by CROWs were proposed. The wave amplitude decays exponentially as it moves away from the defect, enabling strong localization and low group velocity transmission¹⁹ of waves in CREWs. Theoretically, CREWs can be designed for arbitrary acoustic lines.^{20–22} Wang *et al.* realized multiple bending waveguides based on CREWs.^{17,23} Ji *et al.* proposed a CRAW

model by arranging scatterers made of square shape memory alloy in a water matrix.²⁴ Escalante *et al.* investigate the dispersion of CRAW formed by evanescent coupling of a chain of defect cavities.²⁵

Although PCs exhibit the properties discussed earlier, they rarely have real-life applications. Most PC-based devices operate in fixed frequency ranges. The material and geometrical parameters are hardly tunable or reconfigurable after fabrication. Since elastic wave propagation is mainly controlled by material properties and geometry parameters, extensive research has been conducted on tunable and reconfigurable manipulation of acoustic and elastic waves. Tunable phononic crystals¹ achieve control over material parameters through physical fields, such as altering the electric field,²⁶ magnetic field,²⁷ thermal field,²⁸ etc. Reconfigurable phononic crystals,²⁹ on the other hand, modify their geometric structure through mechanical means, changing the magnitude of prestress in the structure,³⁰ introducing fluid into predetermined holes,^{31,32} or other methods to control wave propagation.

In this Letter, we demonstrate a fascinating approach for demultiplexing Lamb waves in the frequency and space domain using reconfigurable CREWs. Reconfigurable defects are introduced by fastening threaded rods with nuts to a perforated two-dimensional phononic crystal slab. Two types of defects are defined based on the assembly length of the rod, so that the latter resonates at different frequencies. By coupling parallel waveguides, space and frequency demultiplexers

operating at resonant frequencies are designed and fabricated. Manipulation of Lamb waves is accomplished through discontinuous defect chains. Finite element analysis is employed for numerical simulations, and it is found that experimental and numerical results are in agreement, with minor deviations in the resonant frequency. This work is essential for the design and application of reconfigurable phononic devices.

Figure 1 depicts the experimental setup. The assembly length L is defined as the distance between the top of the threaded rod and the lower surface of the upper nut, relative to the positive direction of the z -axis of the reference system. Defects are labeled either as type A ($L = 6$ mm) or type B ($L = 9$ mm) according to their length L . a is the lattice constant. Each threaded rod is clamped to the slab by four nuts, symmetrically placed on each side slab. A digital torque wrench (measurement range: 0.2–10 N.m, measurement accuracy: 2%) is used to apply a consistent prestress to the assembly of the rods. In the experiment, we apply a prestress of 3.5 N.m to all rods to ensure proper clamping.²⁹ In the numerical calculations, we apply a prestrain of 0.0067 to all rods as a corresponding boundary condition.

Lamb waves are excited via two piezoelectric patches (PZTs) symmetrically attached to the slab. Two vertically polarized patches are linked in opposite directions. The utilization of two patches enhances the excitation of out-of-plane vibrations. Before being applied to the PZTs, the excitation signal is amplified. Considering the limited lateral range of the excitation source, in-plane modes are inevitably excited as well.¹⁶ A Polytec PSV-500 scanning vibrometer was used to detect and image propagating Lamb waves. Step or fixed frequency harmonic signals are utilized respectively to measure the frequency response and displacement distributions.

Numerical simulations are conducted using the 3D (3-dimensional) finite element software COMSOL. Periodic Bloch boundary conditions are applied along the x and y directions, and other interfaces are set as traction-free. Eigenmodes are obtained by selecting relevant frequencies. To distinguish different polarization

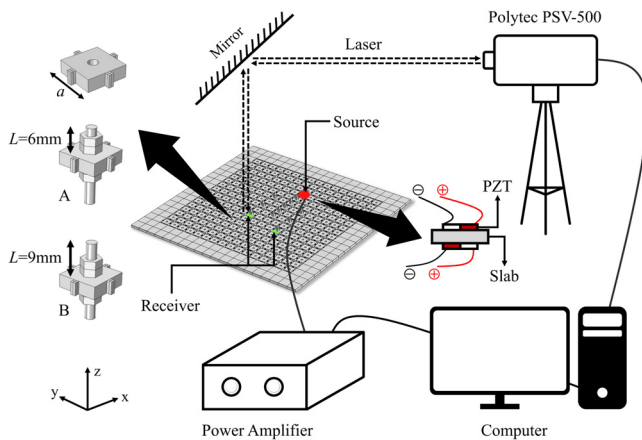


FIG. 1. Experimental setup for excitation and imaging of coupled-resonator defect chains. Two piezoelectric patches (PZTs) are attached to opposite sides of the slab and connected to a power amplifier to serve as a Lamb wave source. The source position is indicated by the red disk, whereas the receiver segment positions are indicated by the green blocks. Vibrations are detected using a scanning vibrometer (Polytec PSV-500). Unit cells of the perfect PC slab and defects A ($L = 6$ mm) and B ($L = 9$ mm) are shown as insets.

modes,³³ we calculate the ratio of the out-of-plane displacement to the squared total displacement via

$$p_z = \frac{\int |w|^2 dV}{\int (|u|^2 + |v|^2 + |w|^2) dV}, \quad (1)$$

where (u, v, w) represent the three components of displacement in the reference system in Fig. 1. Transmission properties are calculated by evaluating the frequency response function (FRF) as

$$T(f) = \frac{\int_{S_1} U_1 ds / S_1}{\int_{S_0} U_0 ds / S_0}, \quad (2)$$

where $U_0 = 1$ is the amplitude of the wave source at the excitation source (S_0) and U_1 is the total displacement collected over a receiver segment (S_1) placed at the end of the waveguide. The numerical results indicate that boundary reflections have a minimal effect on the transmission peaks. In order to reduce the noise and, thus, facilitate the determination of the location of the transmission peaks, low-reflective boundaries are set in the simulation. Elastic wave source and the receiver segments are set inside the slab.

First, we investigate defect modes with threaded rods and nuts. Supercells (size $9a \times 9a$) are formed to calculate the resonant frequencies of the isolated defect modes. The coupling between adjacent defects can be neglected since the size of the supercells is large enough.¹⁷ When the threaded rod is clamped on the slab with $L = 6$ mm, the original symmetrical structure is broken, resulting in a resonant frequency at 67 kHz. Figure 2(a) shows the eigenmodes for

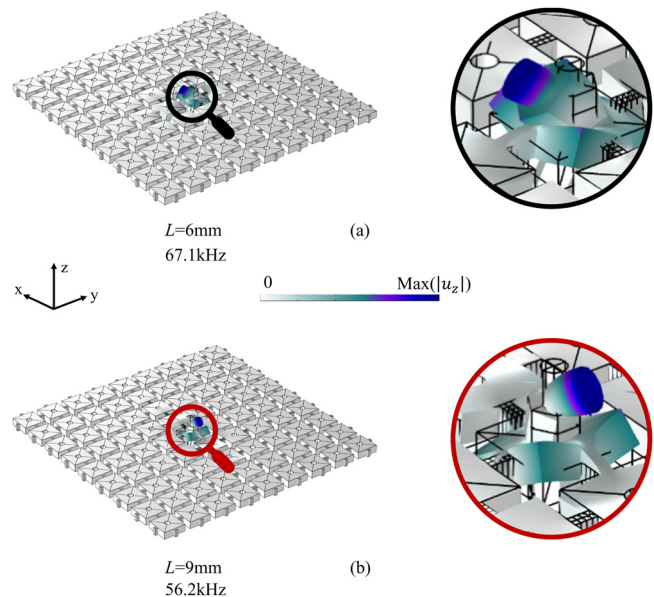


FIG. 2. Displacement fields of the defect modes for defect A ($L = 6$ mm) and defect B ($L = 9$ mm). Eigenmodes at selected frequencies are displayed in panels (a) and (b). The color scale represents the normalized amplitude of the z -displacement from zero (white) to maximum (blue).

defect A at selected frequencies. It is observed that both the top and the bottom free end of the rod vibrate in a bending motion typical of a clamped-free beam. The mode is, in fact, degenerate in the x and y directions and can contribute to wave transmission.

When the assembly length is increased to $L = 9$ mm, the resonance frequency shifts downward to 56 kHz. The degenerate eigenmode for defect B is of the same type as for defect A, as shown in Fig. 2(b); it also contributes to wave transmission. The alteration in assembly length modifies the distribution of rods length on either side of the slab. This leads to a change in the effective length of the rods, hence to a shift in the resonance frequency. This model explains that by manipulating the assembly length $L = 9$ mm of the defects, tunability of the resonant frequency can be achieved in the PC slab.

By coupling three parallel CREWs ($L = 6$ mm, indicated with blue wireframes), we form a spatial demultiplexer as shown in Fig. 3(a). The demultiplexer has a length of $7a$ and a width of $5a$; each CREW has a length of $5a$. The numerical FRFs measured at the two receiver segments of the demultiplexer are presented in Figs. 3(b1) and 3(b2). We can clearly observe that the transmission peaks are obtained around 67 kHz, corresponding to the defect mode. Figures 3(c1) and 3(c2) present the experimental FRFs. The P1 and P2 channels have the same resonance frequency. To ensure the consistency of both channels, we add filtering to reduce signal noise and reflective stickers to the slab surface to guarantee a consistent board flatness. At 55 kHz, additional transmission peaks emerge in the experimental FRFs. These deviations may be attributed to the imperfect adhesion between PZT and slab,

resulting in the excitation and pickup of an in-plane mode of defect A. The other observed differences may be attributed to imperfect assembly of the rods to the slab, since the threaded structure was not considered in the simulation.¹⁷

Numerical and experimental displacement field at the selected frequencies are shown in Figs. 3(b3) and 3(c3). The wave source is placed on the left side of the demultiplexer. Elastic waves first propagate along the central CREW. Then, they couple to the upper and lower waveguides, and energy is split between channels P1 and P2. The polarization of the waves is in accordance with the polarization of the defect mode. Lamb waves are tightly localized within the coupled waveguides, thereby enabling spatial demultiplexing.

As shown in Fig. 4(a), we form a frequency demultiplexer consisting of defects of type A ($L = 6$ mm, indicated with a red wireframe) and type B ($L = 9$ mm, indicated with a blue wireframe). The middle channel, N2, is made up of interleaved defects. Two CREWs (N1 and N3 channels) are placed on either side of the N2 channel, each of the three channels has a length $5a$. The frequency demultiplexer has a total length of $7a$ and a width of $5a$, as the spatial demultiplexer.

Figures 4(b1) and 4(b2) display the numerical FRFs obtained at the two receiver segments of the demultiplexer. The FRF within the resonant frequency band is due to the defect modes. It is worth noting that the peak around 56 kHz for channel N1 does not align with the bandgap. Furthermore, an additional peak at approximately 67 kHz is evident for channel N3. These frequencies, 56 and 67 kHz, represent passing bands for their respective channels. This observation implies

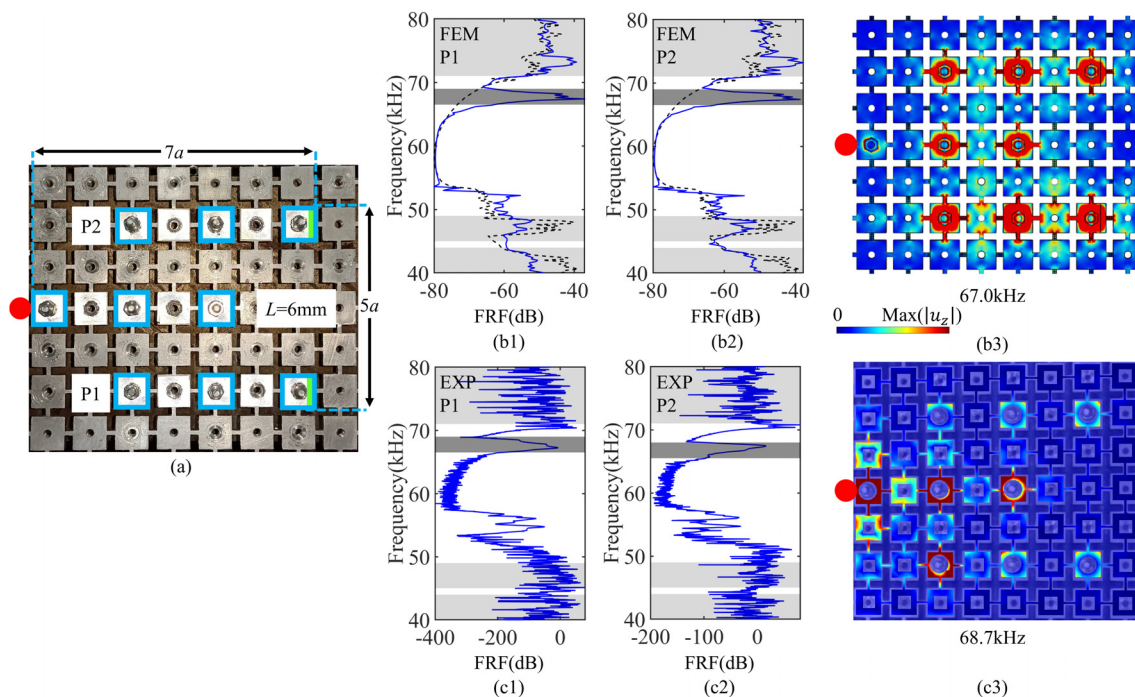


FIG. 3. Spatial demultiplexer. (a) Photograph of the sample. Numerical and experimental FRFs are shown in panels (b1), (b2), (c1), and (c2). The FRF for the perfect PC slab is plotted with a black dashed line in (b1) and (b2) for comparison. The dark-gray color marks the guiding bands. The light-gray color marks the passing bands for out-of-plane polarized waves in the perfect PC slab. Numerical and experimental displacement fields at selected frequencies are displayed in panels (b3) and (c3). The position of the wave source is indicated by the red disk. The positions of the receiver segments are indicated by the green blocks. The color scale represents the normalized amplitude of the z -displacement from zero (blue) to maximum (red).

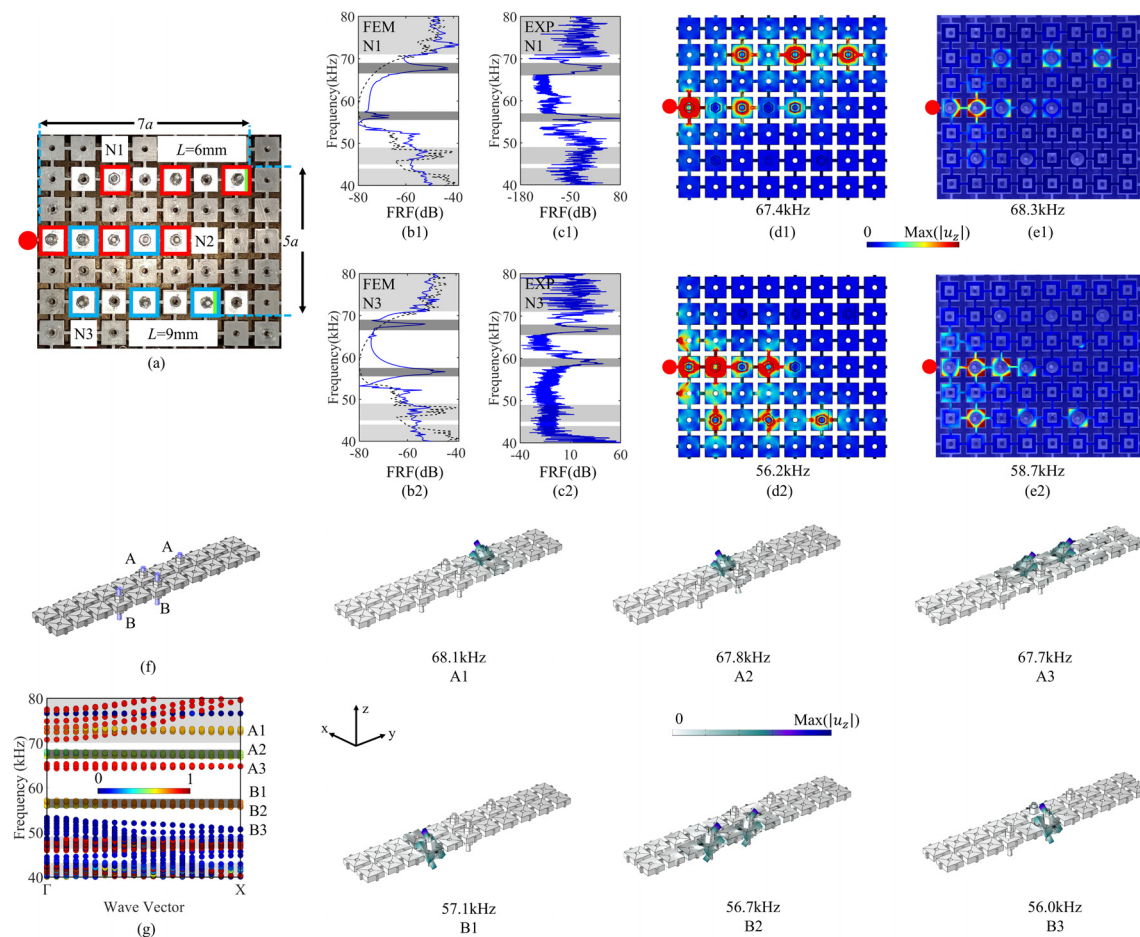


FIG. 4. Frequency demultiplexer. (a) Photograph of the sample. Numerical and experimental FRFs are shown in panels (b1), (b2), and (c1), (c2). The dark-gray color marks the guiding bands. The light-gray color marks the passing bands for out-of-plane polarized waves in the perfect PC slab. The FRF for the perfect PC slab is plotted with a black dashed line in (b1) and (b2) for comparison. Numerical and experimental displacement fields at selected frequencies are displayed in panels (d1), (d2) and (e1), (e2). The wave source position is indicated by the red disk. The receiver segment positions are indicated by the green blocks. The color scale represents the normalized amplitude of the z-displacement from zero (blue) to maximum (red). Coupled-resonator supercell (f) formed on the basis of perfect PCs with defect A and defect B. The band structure (g) of the supercell was computed. The color bar represents the polarization from 0 (blue) to 1 (red). The light-gray areas mark the passband for the out-of-plane mode of a perfect PC slab. The dark-gray areas indicate the considered waveguiding bands. Eigenmodes at marked points A1, A2, A3 and B1, B2, B3 are listed on the right. The color scale represents the normalized amplitude of the z-displacement from zero (white) to maximum (blue).

that the coupling between channels may affect each other's response. However, this coupling effect that results in only minor response amplitudes is regarded as having a negligible impact. Different L values correspond to passing bands at different frequencies, causing the channels to resonate separately. Compared to numerical FRFs, the experimental FRFs in Figs. 4(c1) and 4(c2) show deviations in the transmission peak frequency, resonant bandwidth, and response amplitude. As with the spatial demultiplexer, the PZTs excite an in-plane mode of defect A in experiment, resulting in a higher transmission of the N1 channel at 56 kHz in Fig. 4(c1). In Fig. 4(c2), the N3 channel exhibits a higher resonance frequency around 56 kHz. This may be attributed to the symmetry of the structure of defect B. The symmetry of the structure causes N3 channel to excite higher resonance frequencies in experiments.²⁹ During the construction process, some assembly defects were also identified between the rods and

slab. Non-uniform distribution of force applied by the nuts on the rods can result in variations in the defects. These may, in turn, lead to deviations in the experimental outcomes.³⁰

Numerical and experimental displacement fields at the selected frequencies are shown in Figs. 4(d1), 4(d2), 4(e1), and 4(e2). The wave source is placed to the left side of the demultiplexer. Elastic waves first propagate along the hybridized channel N2. Subsequently, they couple to either the upper or the lower waveguide, continuing toward channel N1 at 67 kHz and channel N3 at 56 kHz. Nevertheless, the resonance frequencies of channels N1 and N3 experimentally deviate slightly from the numerical values. Anyway, at specific frequencies, Lamb waves are clearly guided along only one of the defect chains, thereby enabling frequency demultiplexing.³⁴

To better explain the coupling between the waveguides, we formed a supercell (size $2a \times 11a$) in Fig. 4(f). In the supercell, two

defects of type A and two defects of type B are arranged according to the pattern used for the waveguides of the frequency demultiplexer. The band structure for the perfect waveguide is presented in Fig. 4(g), together with the defect bands for defects A and B. The presence of both red and blue bands indicates that their polarization is mixed. Two defect bands appear close to 56 and 67 kHz, in accordance with the frequency of the defect modes shown in Fig. 2. The deaf band at 65 kHz is not discussed here. Observing the eigenmodes at points A1, A2, A3 and B1, B2, B3 in Fig. 4, around 56 kHz, it can be concluded that defects of type B are resonating, whereas defects of type A exhibit the vibrational form of the bandgap. Around 67 kHz, in contrast, defects of type A are resonating, whereas defects of type B exhibit the bandgap vibrational form. All eigenmodes are, in fact, degenerate in the x and y directions, and both can contribute to wave transmission. This supercell analysis illustrates how the frequency demultiplexer operates.

In this Letter, we have presented a method for demultiplexing Lamb waves in the frequency or the space domain, based on reconfigurable coupled-resonator elastic waveguides. Through manipulation of the assembly length of threaded rods, we initially formed two different resonators with a single point defect. We then designed and fabricated wave demultiplexers. By coupling waveguides, we can modulate Lamb waves at resonant frequencies of the defects. Experimental results agree fairly well with numerical results in all cases. The present study confirms the possibility of reconfigurable wave manipulation in phononic metaplates through the coupled resonance effect. Phononic circuits operating at various frequencies can be achieved through a simple approach without the need to redesign the supporting metaplate. This type of frequency demultiplexer may have applications in signal processing. Furthermore, these findings could also be a basis for the development of advanced active and intelligent acoustic devices.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Yi-Ming Cui and Hao-Ran Dong contributed equally to this work.

Yi-Ming Cui: Data curation (equal); Software (equal); Writing – original draft (equal). **Hao-Ran Dong:** Data curation (equal); Software (equal); Writing – original draft (equal). **Yan-Feng Wang:** Conceptualization (equal); Project administration (equal); Supervision (equal). **Vincent Laude:** Funding acquisition (equal); Validation (equal); Writing – review & editing (equal). **Yue-Sheng Wang:** Funding acquisition (equal); Project administration (equal); Writing – review & editing (equal).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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