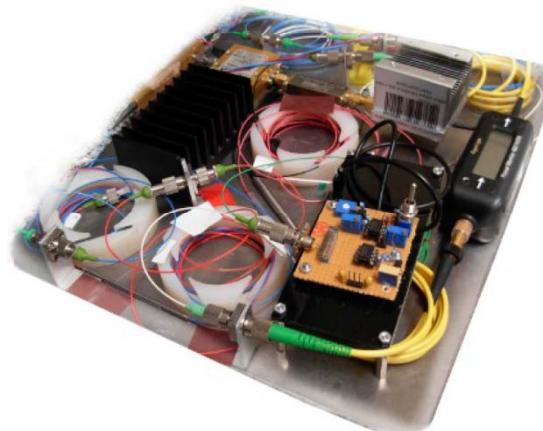




10 GHz bandwidth nonlinear delay electro-optic phase dynamics for ultra-fast nonlinear transient computing

A. Baylón-Fuentes, R. Martinenghi, M. Jacquot, Y. Chembo and L. Larger
FEMTO-ST/ Optics department, UMR CNRS 6174, Université de Franche-Comté, Besançon, France



phocus
towards a PHOtonic liquid state machine
based on delay-CoUpled Systems



CLEO / Europe IQEC 2013, CD-10: Optical Devices for Data Processing
12 – 16 May 2013, Munich, Germany

LabeXaction
Integrated smart systems



femto-st
SCIENCES &
TECHNOLOGIES

CLEO / Europe IQEC 2013, 12 – 16 May 2013

Outline



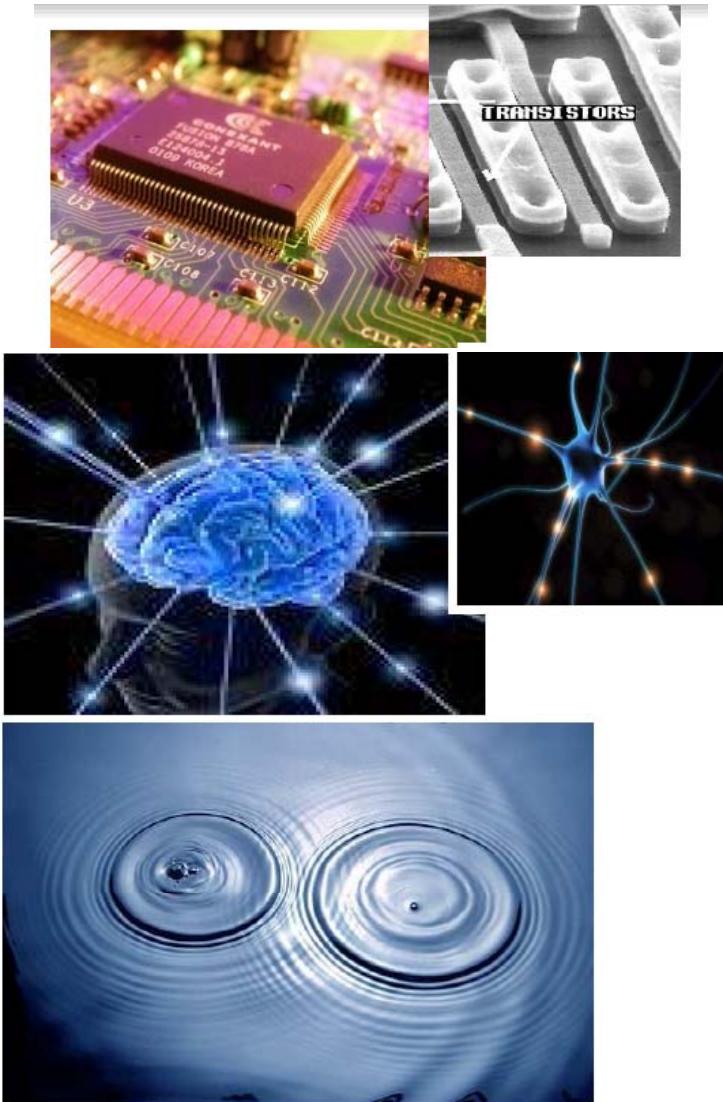
- **Introduction**
 - Background, Motivations
 - Reservoir Computing using delay dynamics
 - High Complexity Delay Dynamics Reservoir with EO
- **RC with Ultra-fast Photonic Nonlinear Delay Dynamics**
 - EO phase Dynamics as a reservoir
 - Operating Conditions of the reservoir
 - Spoken digit recognition test
- **Conclusion, Perspectives**

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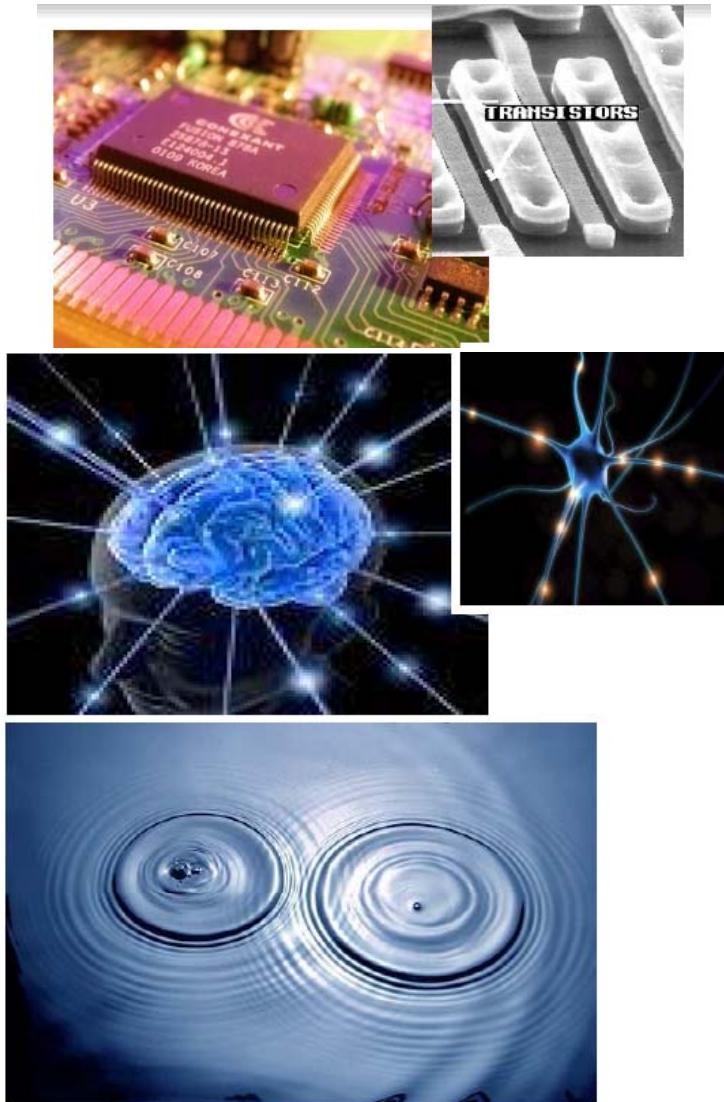
Background, motivations



- **Digital electronics, standard computers are still limited :**
 - ✓ Complex tasks : classification, prediction
 - ✓ Information processing at ultra high speeds.

- **Experimental implementation of Reservoir Computing (RC) or Nonlinear Transient Computing (NTC)**
- **To generate transient states for processing the information**

Background, motivations



- **Neural Network Computing**
 - ✓ Artificial intelligence, network of coupled oscillators, learning, actual demonstration via “conventional computer” simulations
- **Cognitive brain research, bio-inspired computing principles**
 - ✓ biologic neural network, time trajectories corresponding to pulse train solutions
- **Echo State Network (ESN), Liquid State Machines (LSM), Reservoir Computing (RC)**
 - ✓ Novel architecture exhibiting universal computational potential

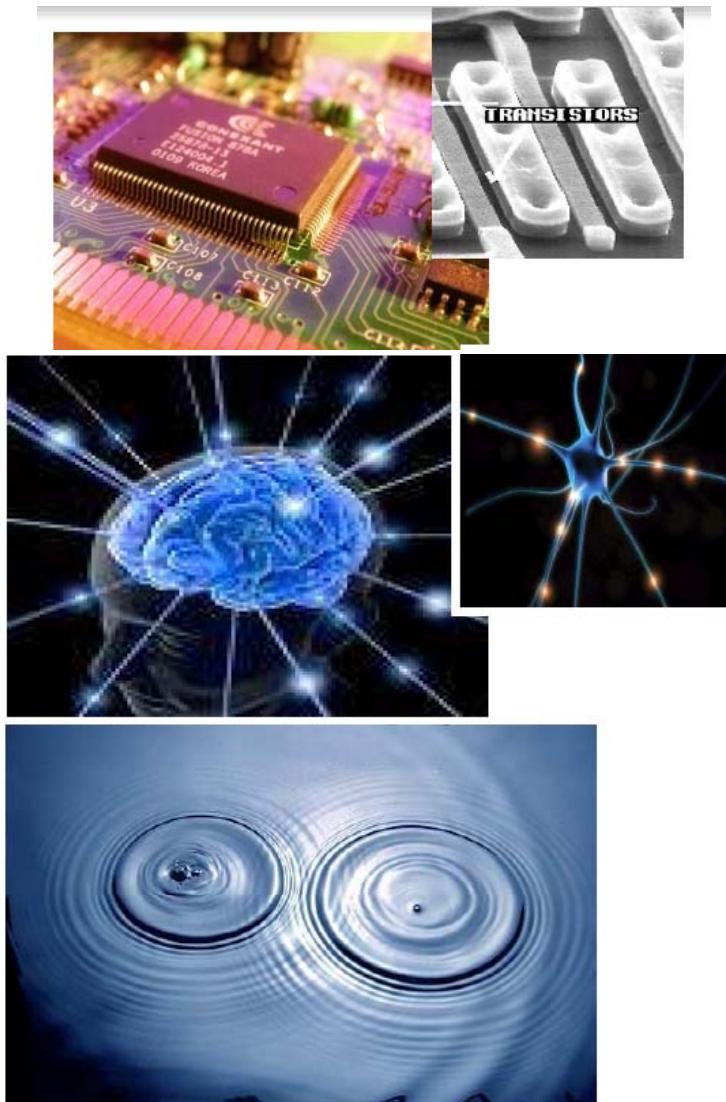
H. Jaeger and H. Haas, “Harnessing Nonlinearity : Predicting Chaotic Systems and Saving Energy in Wireless Communication” Science 304, 78 (2004)

Outline

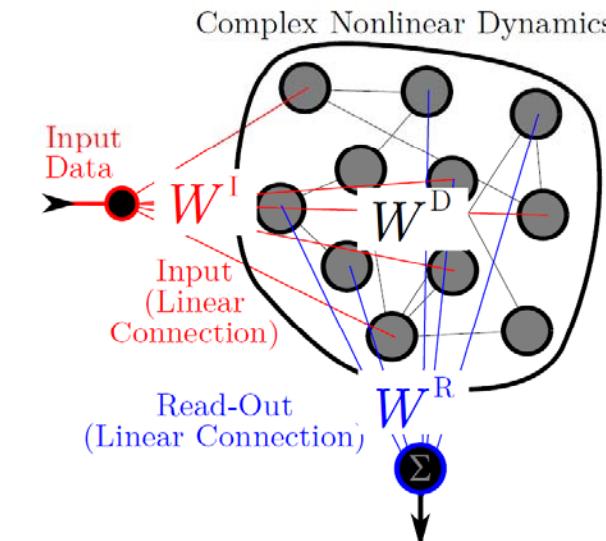


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From Neural Networks to RC



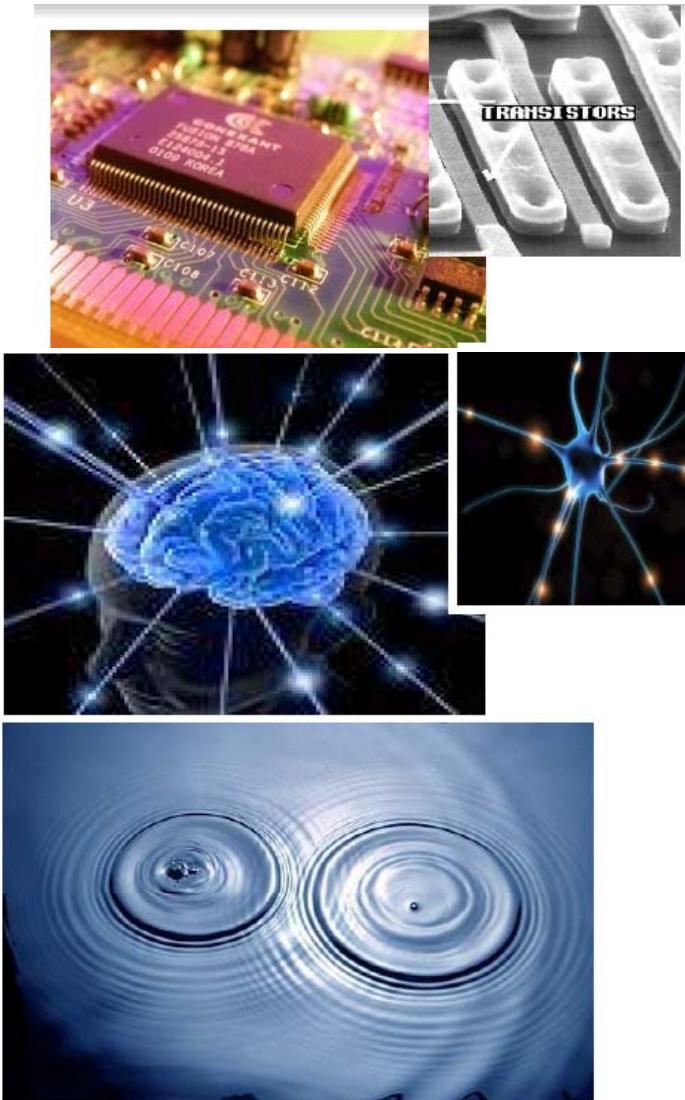
➤ Basic architecture



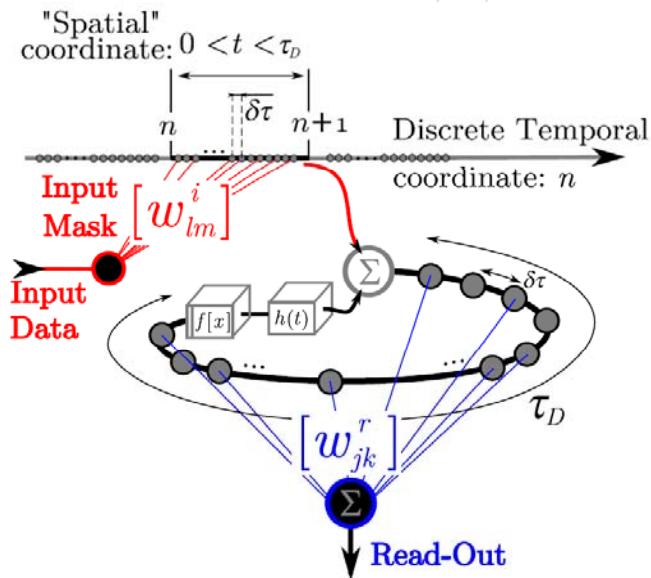
➤ Towards a parallel photonic reservoir :

K.T Vandoorne, J. Dambre, D. Verstraeten, B. Schrauwen, P. Bienstman, "Parallel reservoir computing using optical amplifiers", IEEE Transactions on Neural Networks, 22(9), 1469-1481 (2011)

Our approach : harnessing delay dynamics



➤ Spatio-Temporal viewpoint of a DDE



➤ Towards a reservoir computing experimental setup using delay dynamics :

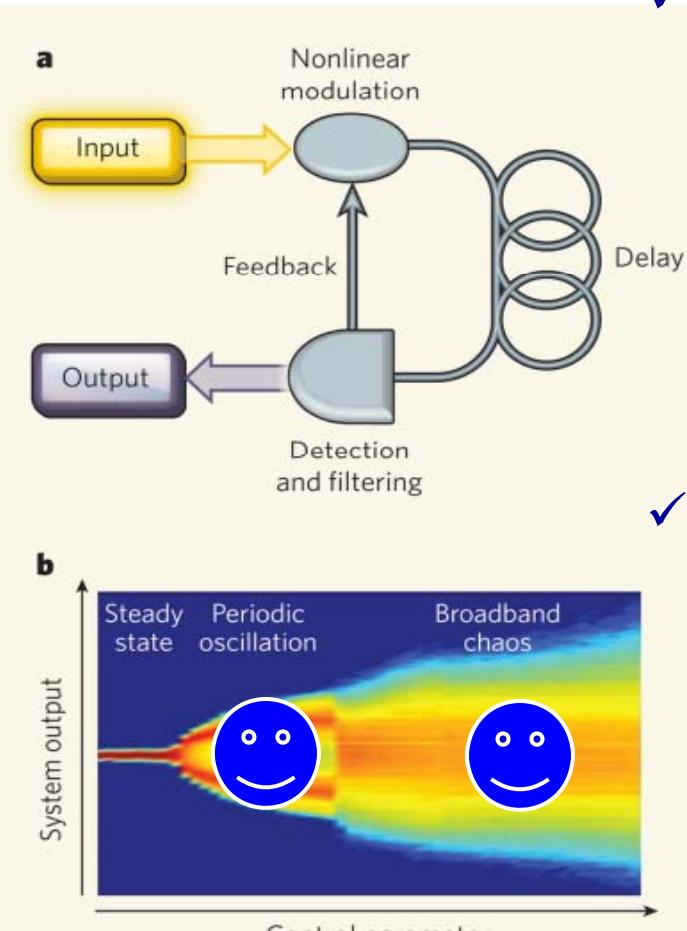
L. Appeltant, M. C. Soriano, G. Van der Sande, J. Danckaert, S. Massar, J. Dambre, B. Schrauwen, C. R. Mirasso, and I. Fischer, "Information processing using a single dynamical node as complex system," Nature Commun. 2, 468 (2011).

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Delay Dynamics with optoelectronic systems



L. Larger, J. M. Dudley, Nonlinear dynamics:
Optoelectronic Chaos, Nature 465, 41-42 (2010)

- ✓ **Ikeda dynamics: linearly filtered nonlinear delayed feedback**

- infinite dimensional dynamics
- very high practical attractor dimension
- highly nonlinear realization
- optoelectronic solution with telecom devices
- high reliability and controllability

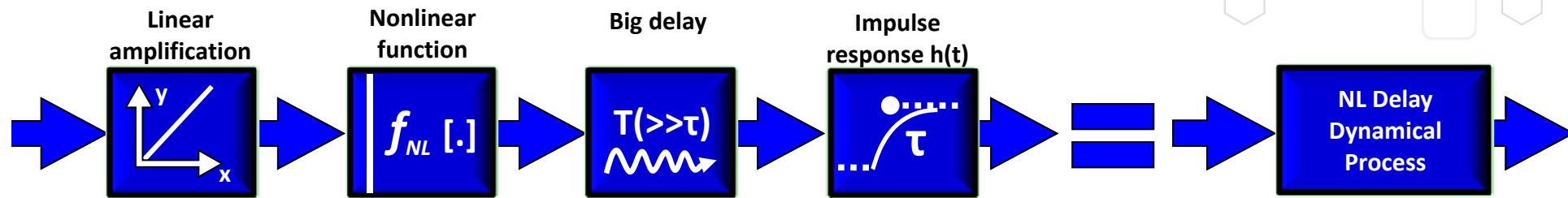
- ✓ **Two Main applications & various regimes vs feedback gain:**

- Optical Chaos Communications
- High spectral purity micro-wave oscillator

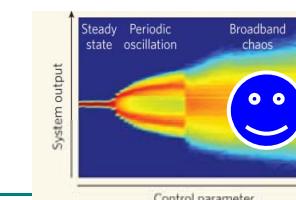
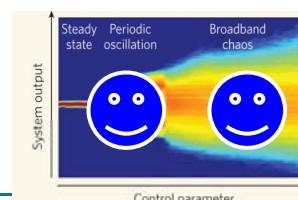
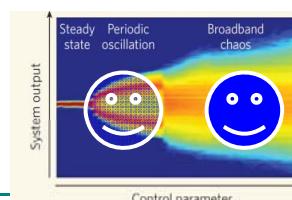
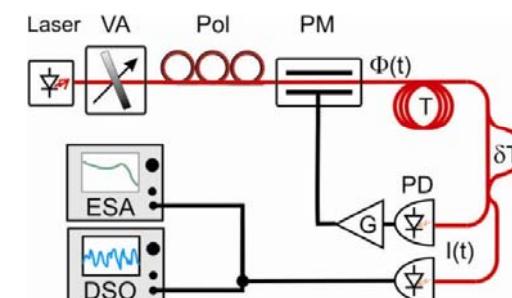
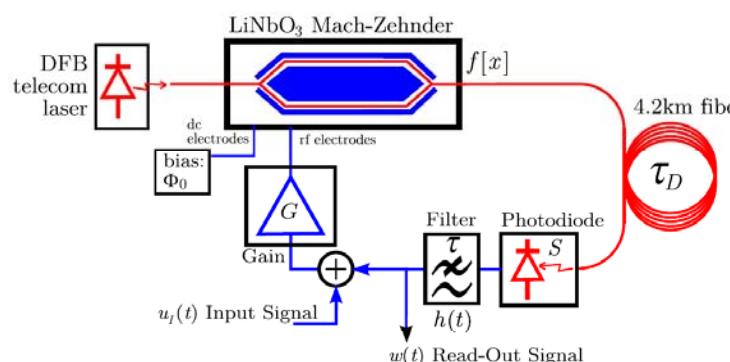
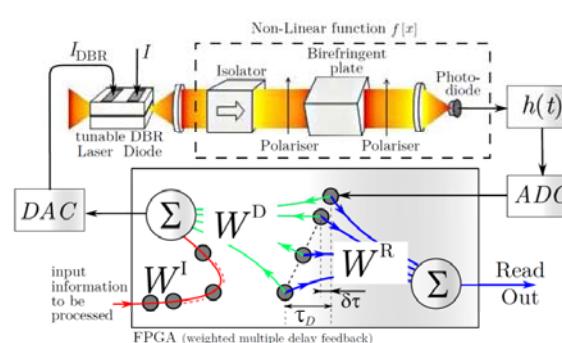
Existing optoelectronic systems



➤ Nonlinear Delay Dynamical Process



➤ Various existing experimental setups



Outline

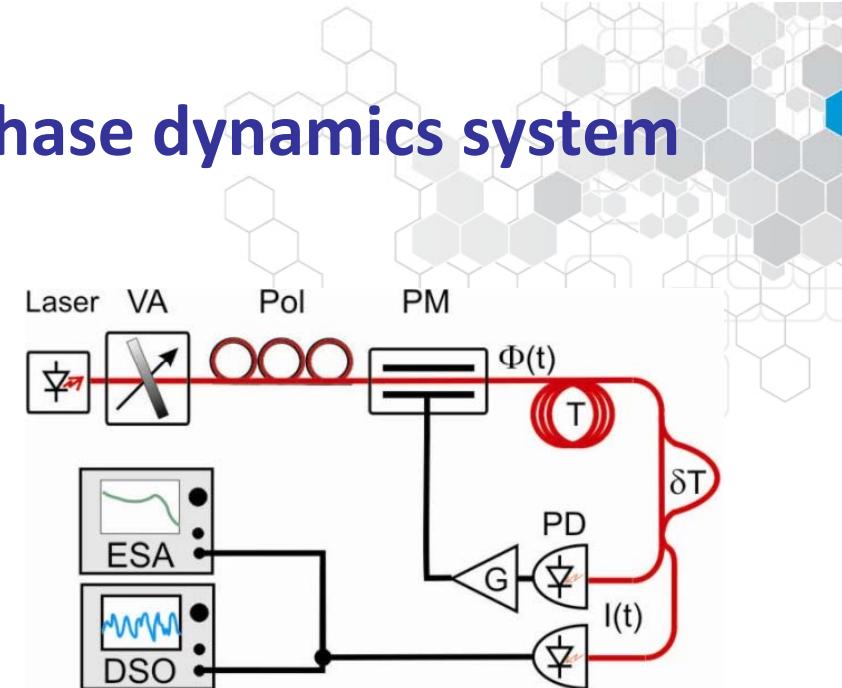


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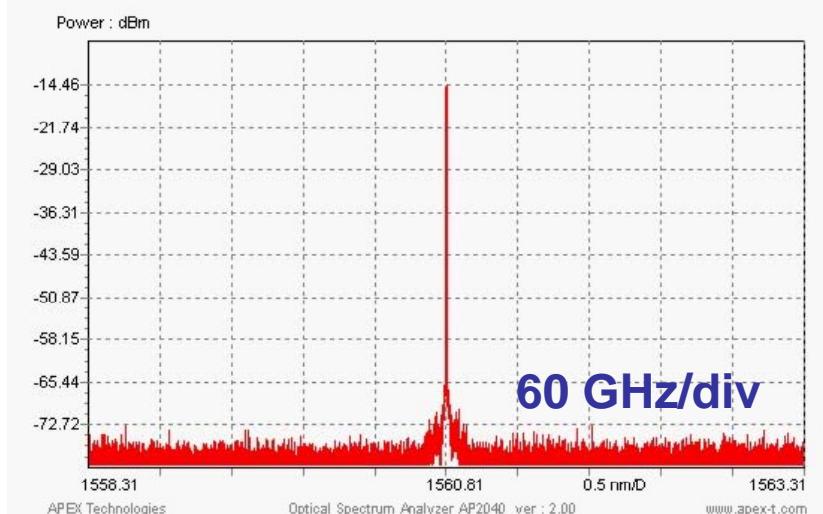
10 GHz bandwidth EO Phase dynamics system

- Picking ideas from efficient coherent communications principles

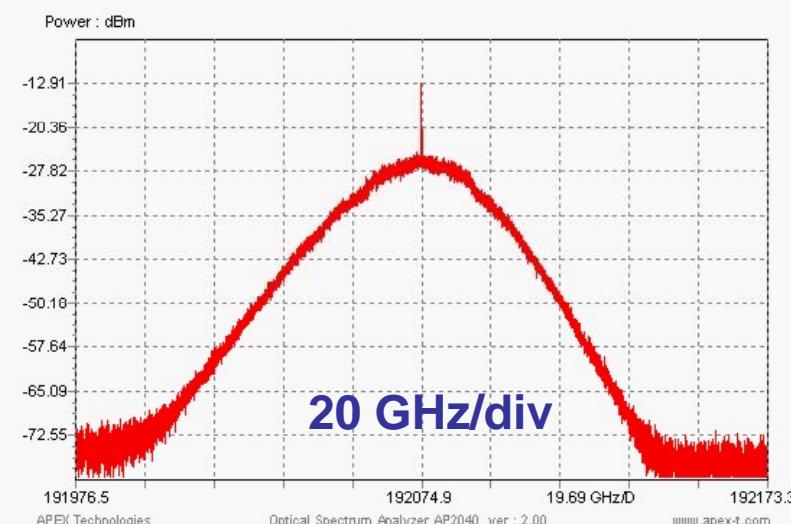
Imbalanced Mach-Zehnder (typ. DPSK demodulator) for PM to IM conversion:
- ca. 3cm unbalancing
- 10Gb/s E/O O/E devices



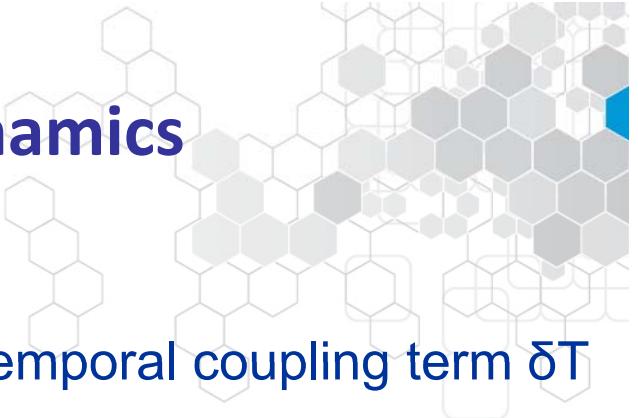
The unmodulated laser



After chaotic phase modulation



EO Phase Dynamics

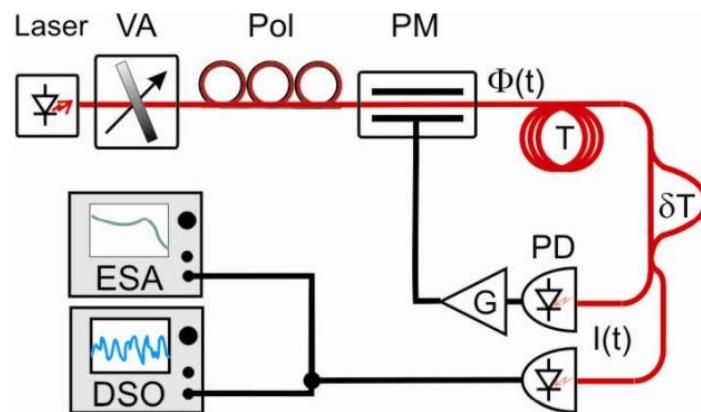


☀ The phase dynamics exhibits an additional temporal coupling term δT

🌀 Nonlinear delay integro-differential equation

$$\frac{1}{\theta} \int_{t_0}^t \varphi(\xi) d\xi + \varphi(t) + \tau \frac{d\varphi}{dt} = \beta \cdot [f_{(t-T)}(\varphi^*) - f(0)]$$

🌀 Imbalanced interferometer: Temporally nonlocal non linearity



* Standard DPSK demodulator:

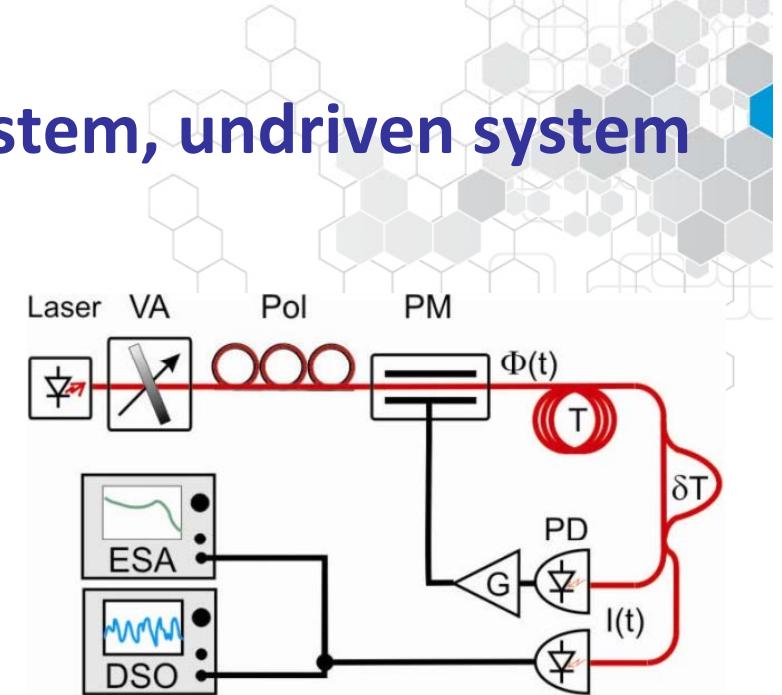
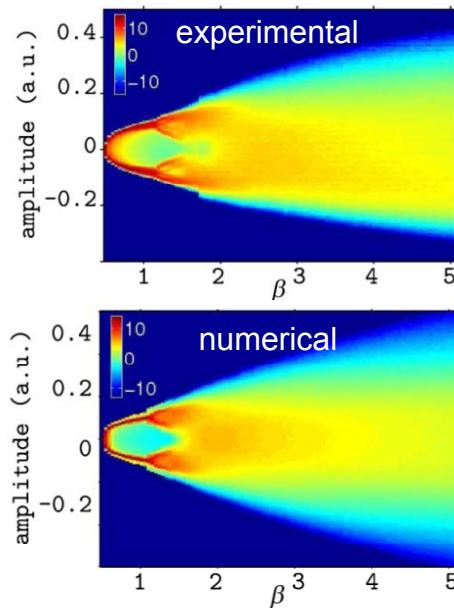
$$f_t(\varphi) = \{1 + \cos[\varphi(t) - \varphi(t - \delta T) + \phi_0]\}$$

* Generalized multiple wave interferometer:

$$f_t(\varphi) = F_0 \left| 1 + \sum_k \alpha_k e^{i[\varphi(t) - \varphi(t - \delta T_k)]} e^{i\phi_k} \right|^2$$

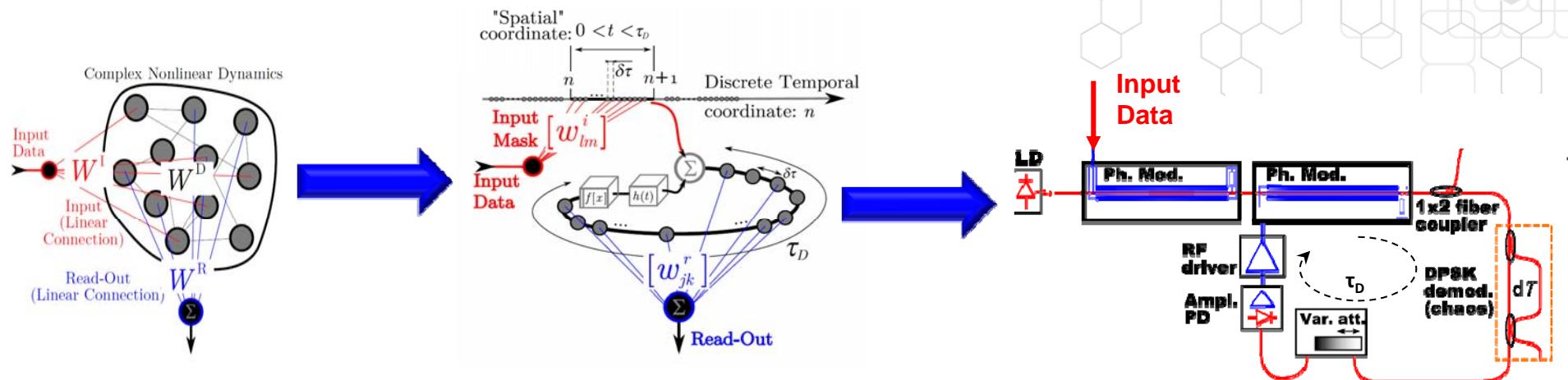
EO Phase dynamic system, undriven system

- Control parameters (feedback gain β , static phase shift ϕ_0) allows to reach complex regime,
- experimental / numerical bifurcation diagrams



Single delay electro-optic phase dynamics, driven system

▪ Basic architecture



- ✓ Photonic setup with a phase dynamic with a bandpass feedback
- ✓ Input Driven Nonlinear Delay Dynamics (DDE):

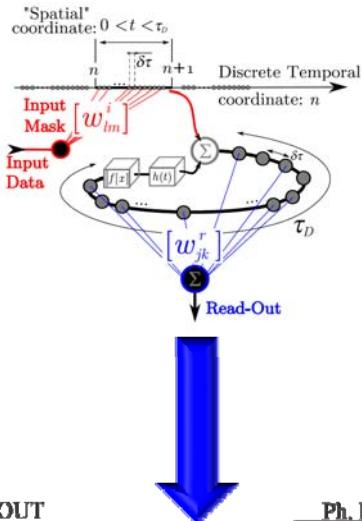
$$\phi(t) + \tau \dot{\phi}(t) + \frac{1}{\theta} \int_{t_0}^t \phi(s) ds = \beta \sin^2 [\phi(t - \tau_D) - \phi(t - \delta T - \tau_D) + \rho u_i(t - \tau_D) - \rho u_i(t - \delta T - \tau_D) + \phi_0]$$

- ✓ Physical variable : response time $\tau \leftrightarrow$ to keep the system far from steady state, $\delta\tau=0,2\tau$
- feedback strength $\beta \leftrightarrow$ overall feedback loop gain; input data weight ρ ; NL operating point $\leftrightarrow \Phi_0$

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Practical values : phase dynamics



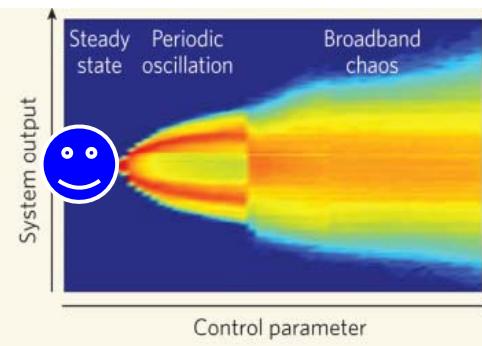
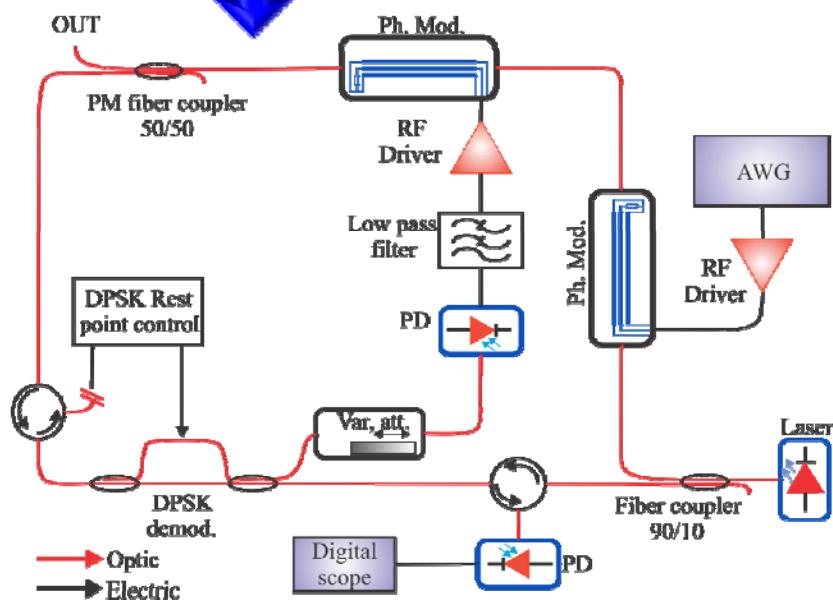
➤ Amplitude parameters :

- ✓ Feedback strength $\beta \approx 0.5$
- ✓ Offset phase Φ_0 : NL operation "close to an extremum"
- ✓ Large input data weight, p_i close to π

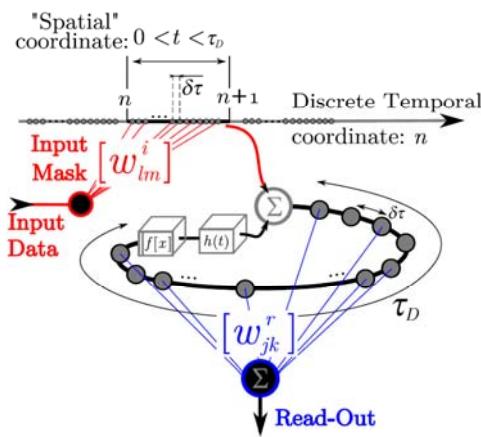
➤ At the edge of chaos... stable steady state

- ✓ Not too small feedback strength β (allowing NL mixing)
- ✓ Not too close to the instability threshold (too slow response)

➤ Nonlinear Transient Computer (NTC)



Practical values : phase dynamics



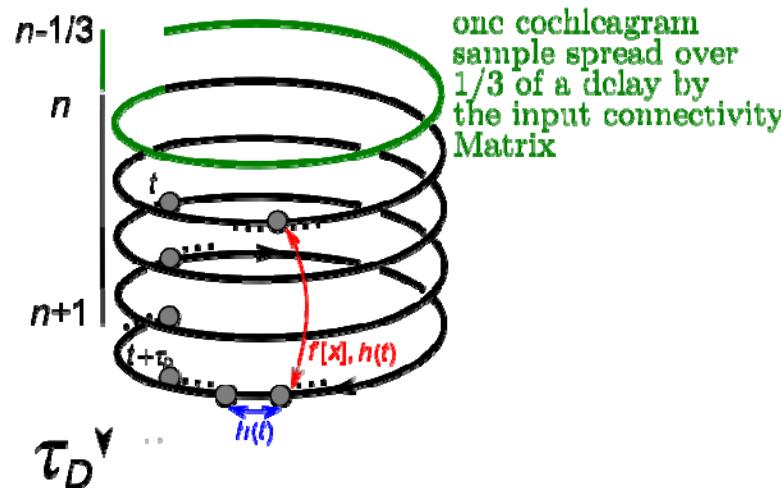
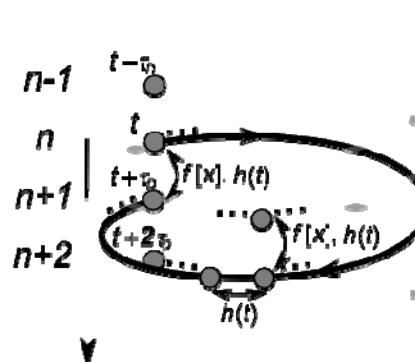
➤ Number of nodes N typically $100 < N < 1000$

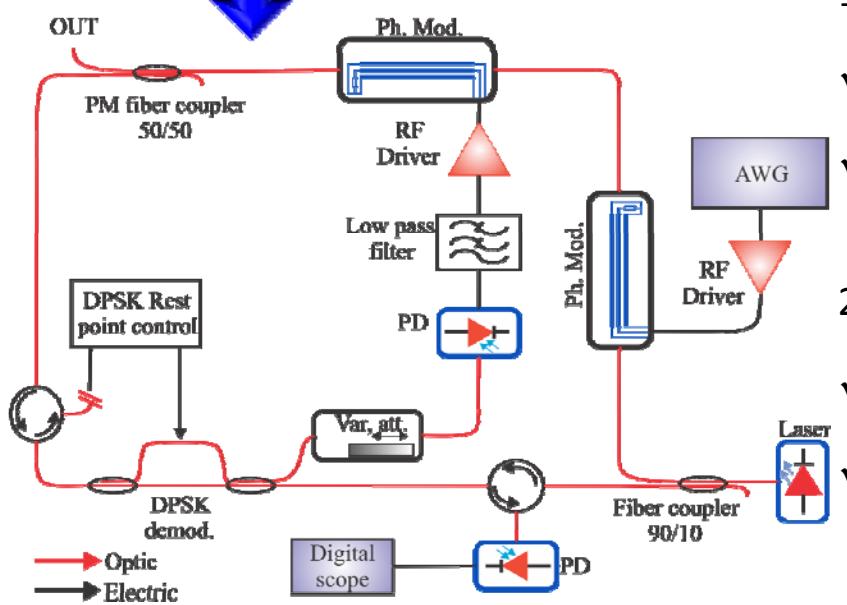
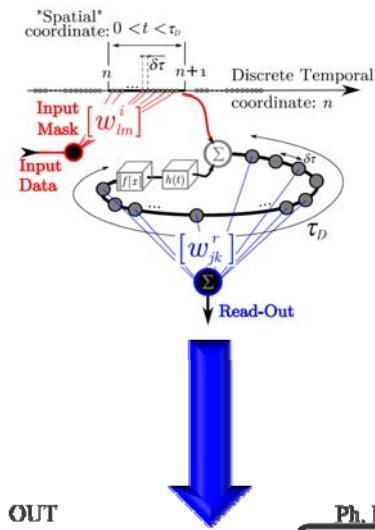
- ✓ to keep the system far from steady state during its dynamical response, we choose $\delta\tau=0.2\tau$ and it gives the number of nodes :

$$N = \tau_D / \delta\tau$$

- ✓ But EO phase system $\tau = 284$ ps , we obtain $N > 1000$, or $\tau = 20$ ps and gives $N > 15000$

To operate with tractable number of Nodes, the input data is spread over 1/3 of the delay (increases the memory): $N = \tau_D / 3\delta\tau = 428$ ($\tau = 284$ ps)





Practical values : phase dynamics

➤ Temporal parameters :

- Fixed delay : $\tau_D \simeq 63.2 \text{ ns}$
- Two different possible low pass filters

1) Intermediate feedback bandwidth $560 \text{ MHz} / \tau = 284 \text{ ps}$

- ✓ Large delay condition, $\tau_D/\tau \simeq 220$, we fix : $\tau_D/3N = 0.2\tau$
- ✓ $N = 428$ nodes separated by ca. 0.2τ : required input and read-out resolution $\simeq 20 \text{ GSamples/s}$

2) Intermediate feedback bandwidth $7.73 \text{ GHz} / \tau = 20 \text{ ps}$

- ✓ Large delay condition, $\tau_D/\tau \simeq 3200$, too large !
- ✓ $N = 428$ nodes separated by ca. 0.2τ (required input and read-out resolution $\simeq 250 \text{ GSamples/s} !!!$)
- ✓ **NOT POSSIBLE WITH OUR AWG and DSO limited to 24 GS/s (AWG) and 45 GHz (DSO),**

but possible in unsynchronized regime (Y. Paquot et al, scientific reports, 2012)

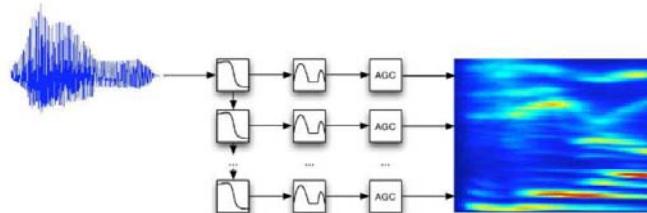
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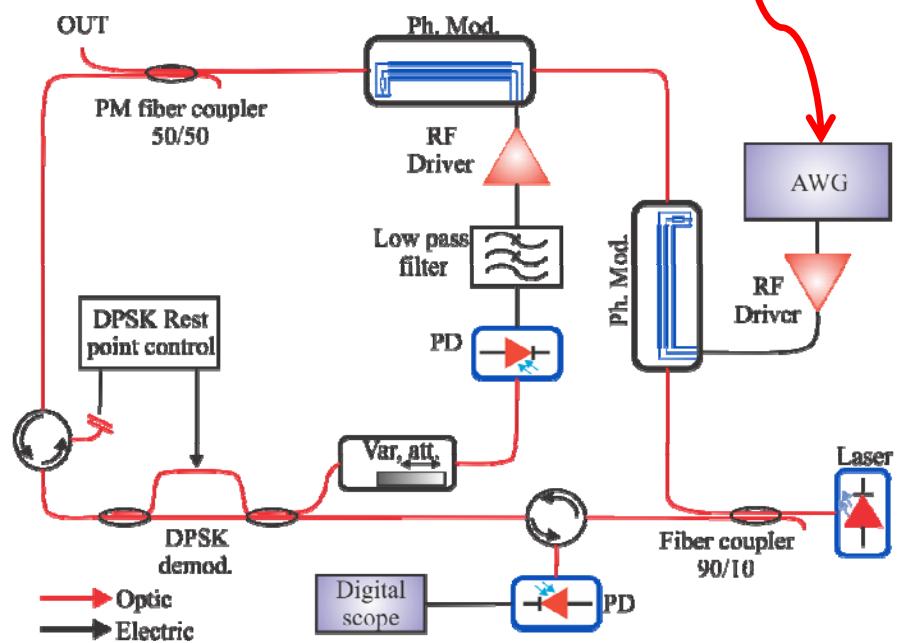
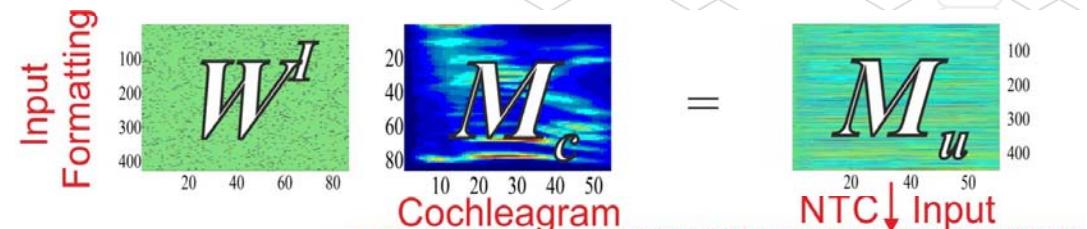
Dynamical Processing of Spoken Digits

➤ Input pre-processing :



Lyon Ear Model transformation (Time & Frequency 2D formatting, 32 to 130 Samples x 86 Freq.channel)

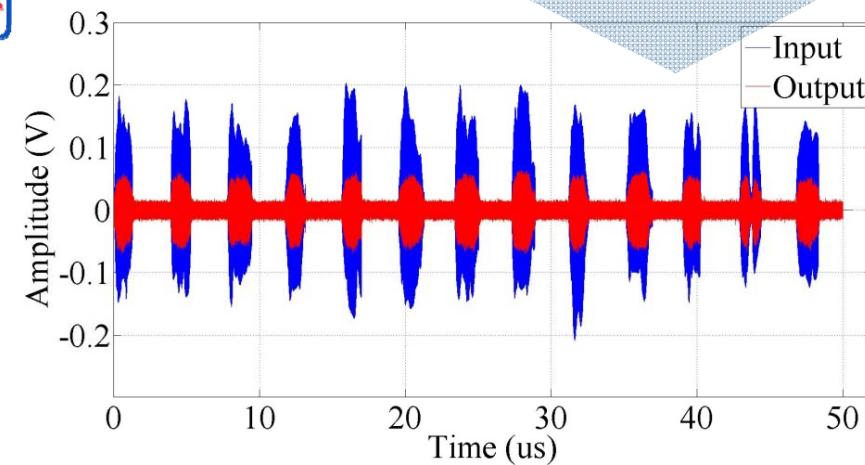
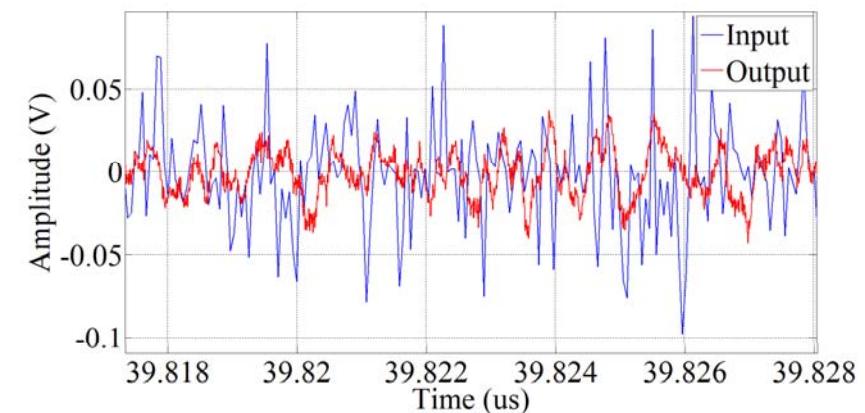
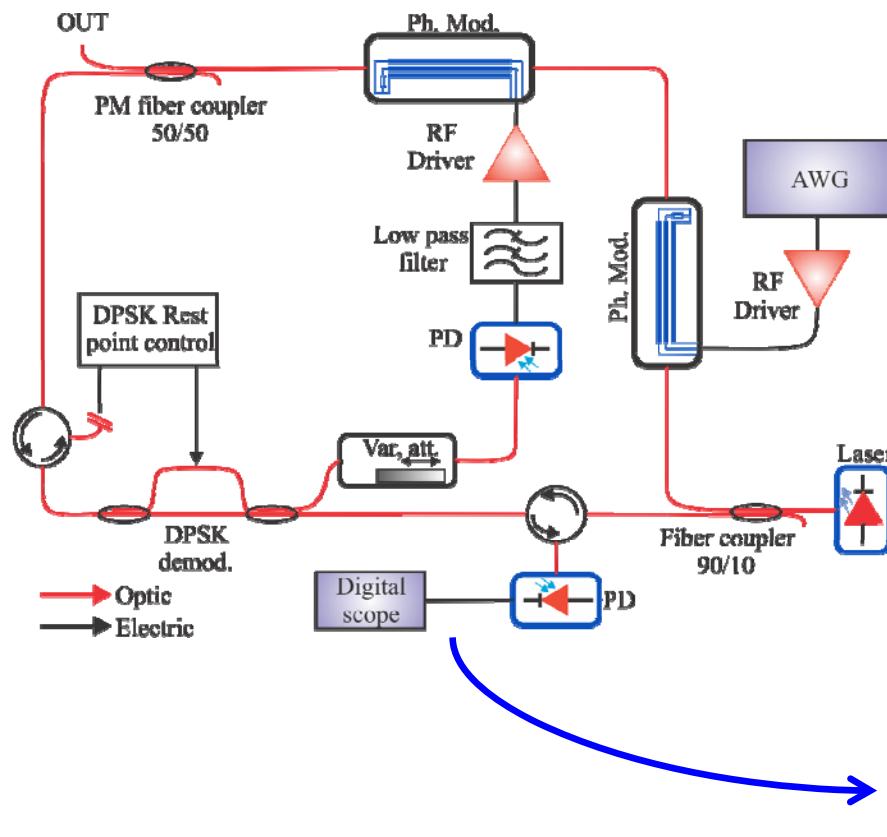
Sparse “connection” of the 86 Freq. channel to the N nodes : random connection matrix



Reservoir state : experimental results

➤ Phase dynamics :

Time series recorded for Read-Out post-processing



Read-Out, Training, and Testing

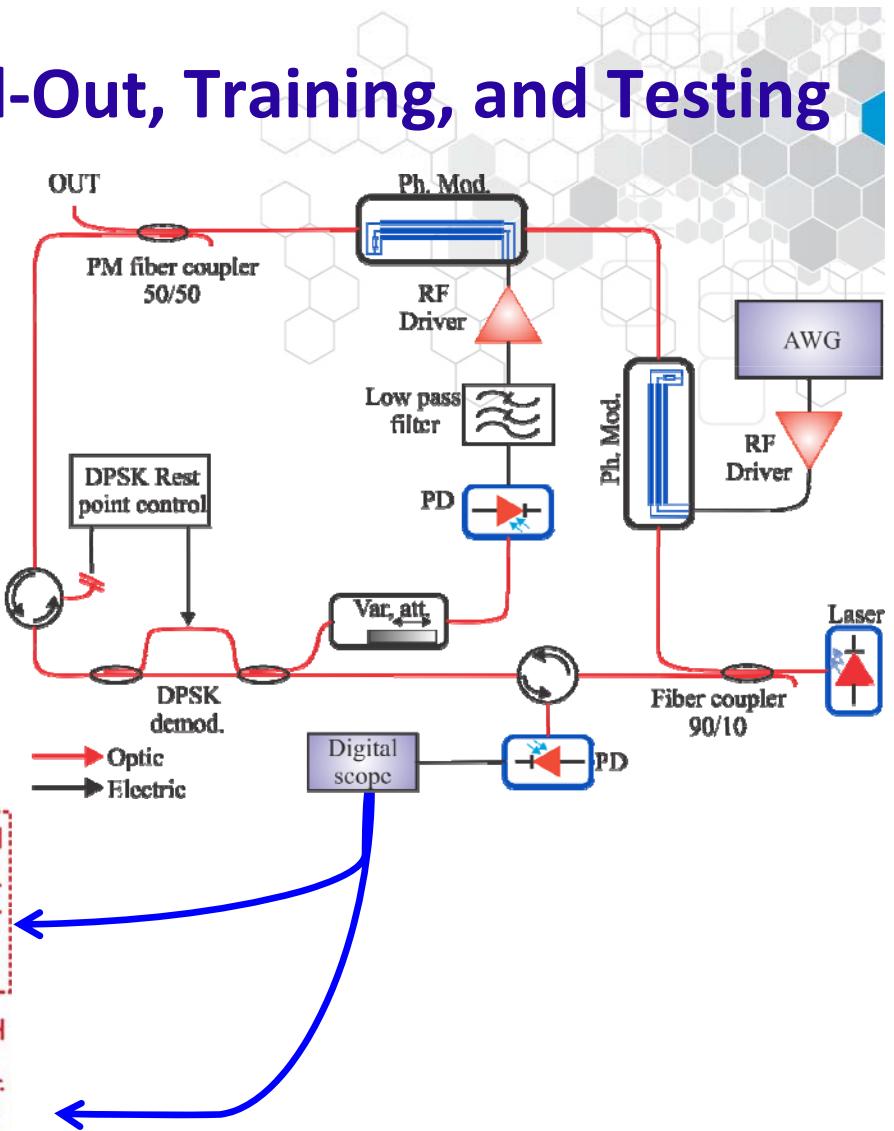
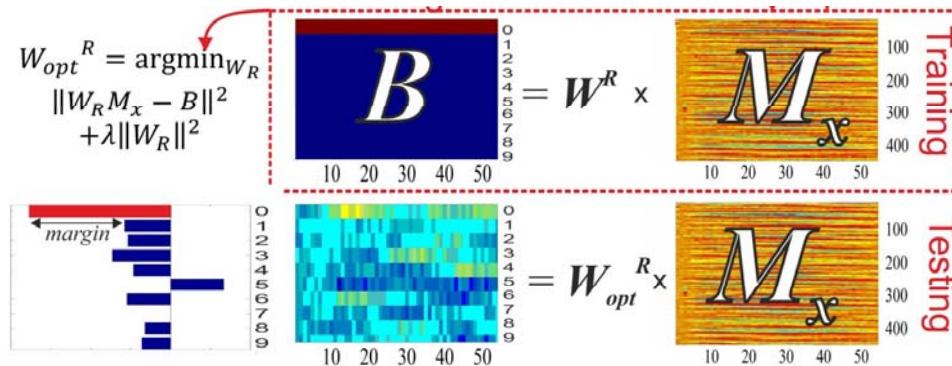
➤ Training of the Read-Out with target output function

Learning: optimization of the W matrix, for each digit

Regression problem

➤ Testing with training-defined Read-Out

Transient response
and post-processing



Results : Word Error Rate (WER) < 0.02% at 20GS/s

We process 1 200 000 spoken digit per second !

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Conclusion, perspectives

- Simple electro-optic architecture with a bandwidth higher than 10 GHz
- Pre- and post-processing performed externally
- Excellent first results at ultra-fast data rate on a classification benchmark test

Spoken Digit Recognition with **Word Error Rate (WER) < 0.02% at 20GS/s, 1.2MDigit/s** (set size limited, 500 spoken digits data base)

Other benchmark test in process (chaotic time series prediction,...)

- Many remaining degrees of freedom for optimization

