

# An example of design, optimization, stabilization and noise performances of resonator-based optoelectronic oscillators

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**Abstract.** In this paper we talk about oscillators of optoelectronic type with intensity modulators and high-quality optical resonators technology. This subject is illustrated by an example of realization from the material to the characterization of the realized oscillator. It is explained how such an oscillator is designed and how it can be optimized.

**Keywords:** Optoelectronic oscillator / optimization / resonator / frequency stability / phase noise measurement

## 1 Introduction

First optoelectronic oscillators (OEO) were developed in the United States [1]. There are some advantages with long delay lines oscillators. Their phase noise can be very low. Ten years ago, Eliyahu et al. [2] reached a phase noise of  $-163$  dBc/Hz at 6 kHz offset from a 10 GHz carrier. The longer the delay line is, the lower the phase noise becomes, but a long delay line is more sensitive to temperature effect. It is a limitation for the phase noise performance. One of the challenges is to have a relatively compact system when designing an OEO. However, a resonator made of a crystal is a good candidate. But coupling a resonator to a line has to be performed accurately. Additionally, mechanical environment must be adequate. Having high  $Q$ -factor (quality factor) resonator aims specified goals such as low phase noise. Optimization signifies finding a way for the improvement of the OEO stability. It works at  $1.55 \mu\text{m}$ . The stabilization of the optical frequency delivered by laser is essential. A technique is particularly used. It consists in Pound–Drever–Hall (PDH) [3]. We found that cells of  $\text{TeO}_2$  (paratellurite) crystal can be used as acousto-optic devices to stabilize a signal delivered in the microwave domain by an OEO. The system developed for the phase noise characterization of the microwave signal generated is then described.

## 2 A crystalline-resonator-based optoelectronic oscillator

### 2.1 Definitions and generalities

In this section, after a bit of history, we remind some important definitions.

John William Strutt (1842–1919) was known as Lord Rayleigh. He was an English physicist. He described origins and transmission of sound waves, and more precisely, phenomena of whispering-gallery-mode (WGM) resonance appearing in Saint Paul's Cathedral dome, located in the capital of England, in his book *The Theory of Sound* [4].

Similar to sound, light propagates by total reflection inside a WGM resonator. In case of an optical path, resonance is a multiple  $p$  of the wavelength  $\lambda$ :

$$L_{\text{OPT}} = p\lambda. \quad (1)$$

Thus, we remind several definitions.

Quality factor  $Q_{\text{OPT}}$  linked to photons lifetime ( $\tau$ ) inside the resonator is

$$Q_{\text{OPT}} = 2\pi\nu_{\text{OPT}}\tau \quad (2)$$

where  $\nu_{\text{OPT}}$  is the carrier frequency.

It means that

$$Q_{\text{OPT}} = \nu_{\text{OPT}}/\Delta\nu. \quad (3)$$

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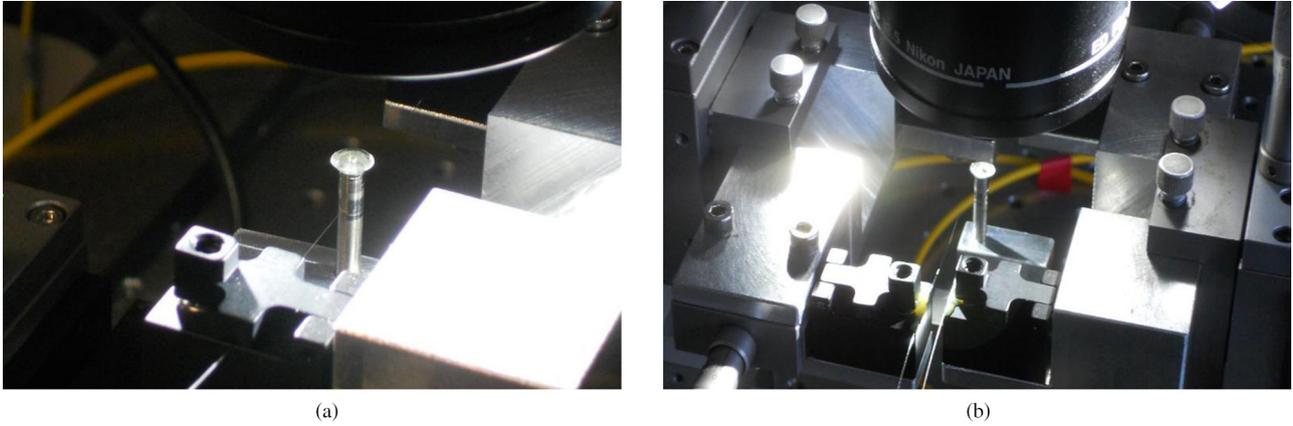


Fig. 1. Coupling process of a 5.5 mm disk resonator by tapered fibers.

The equivalent RF quality factor  $Q_{RF}$  is

$$Q_{RF} = (\nu_{RF}/\nu_{OPT}) Q_{OPT} \quad (4)$$

where  $\nu_{RF}$  is the microwave frequency.

The free spectral range (FSR) determines the range of the microwave signal and is given by

$$FSR = c/2\pi nr. \quad (5)$$

An evanescent field is created, which is useful for a possible coupling. Signal propagates inside the crystal resonator by total reflection. It is called WGM propagation for whispering gallery mode. To obtain a very long delay, the  $Q$ -factor of the resonator must be as high as possible. Microsphere [5] or disk resonators  $MgF_2$  [6],  $CaF_2$  [7] quartz and fused silica [8] give good results and each of them has advantages and limitations. To make a precise estimation of the quality factor, peaks are detected by cavity ringdown characterization [9]. When the quality factor is high enough, photon stays in the resonator for a longer period.

## 2.2 High-quality factor optical resonator

The radius of the resonator is typically 2.5–3 mm. It corresponds to the FSR around 10 GHz.

Grinding is the first step for making concretely the geometry for the guide. Silicon carbide is used for this. Stable table is necessary for avoiding defects due to geometrical variation. The speed at this step can be maximized. The speed is maximized, thanks to a very stable support and an air spinner motor. The next step consists in polishing to decrease roughness of the optical guide. Diamond is used as a powder with dimension less than 1  $\mu m$ . Due to its hardness, every step needs more and more time. As a result, the full process has consequence that the roughness becomes low, down to 2 nm. That is why the quality factor becomes high [10].

## 2.3 Increasing the quality factor of the resonator

Realization of specific electronics and oven are described in references [11,12]. Oven is specially designed. The

temperature is controlled. So the annealing is not too abrupt. It can then increase the  $Q$ -factor for photonics needs by relaxing the surface.

A cylindrical cavity is made of aluminum on its periphery. The muffle chamber is surrounded by a basalt fiber material and inserted inside the oven. Basalt is chopped. It is made of dry, woven noncrimp fabrics fibers. Fibers are milled. So it acts as a heat insulator and blocks fire. Wires are made of resistant alloy nichrome. The main benefit is to let the external surface of the resonator relax while current is passed through the wires.

## 2.4 Installation in OEO

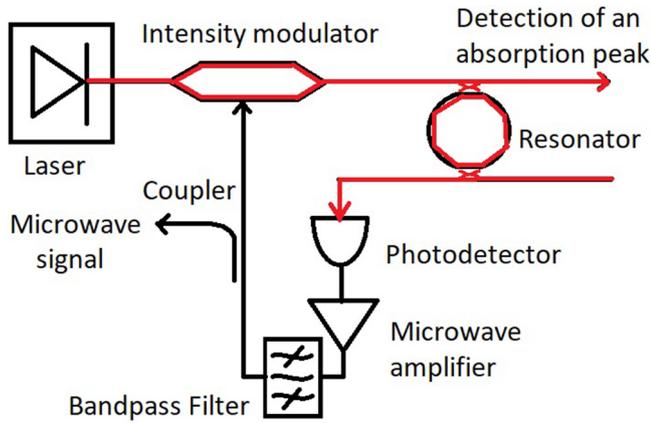
We proceed as follows: In order to couple an optical disk resonator to the first tapered fiber, we proceed by searching the optimized position to produce absorption peaks as is shown in Figure 1a. Then we adjust the coupling position with a second one, as illustrated in Figure 1b, looking at the transmission peaks. Coupling can be optimized [10,13].

## 2.5 WGM resonators

Despite the best  $Q$ -factor up to  $10^{11}$  corresponding to a photon lifetime of 100  $\mu s$  has been achieved in an infrared regime by a team in the United States [14]. Quality factors of  $10^9$  have been achieved [9] with  $CaF_2$  or  $MgF_2$  using mechanical polishing. Modes propagate, thanks to dielectric structures. Modes are strongly confined inside the resonator while they propagate inside the crystal by total internal reflexion. Different shapes are investigated such as circular, spherical and toroidal, and their size is between few micrometers and few millimeters.

## 2.6 Experimental study of the realized OEO

Figure 2 schematizes the principle of OEO. The microwave amplifier compensates the losses in the resonator and the optoelectronic circuit to allow operation in oscillator mode. Note that the optical power delivered by the laser must not be too high (less than 20–40 mW according to the losses) to avoid nonlinearities. The imperfect flatness of the power



**Fig. 2.** Principle of OEO. Red color is used for optical signal and black for microwave signal. Optical signal transmitted through the resonator is detected by the photodetector.

delivered by the amplifier as a function of frequency, and the filtering elements, makes it possible to favor the emergence of a peak, which will be the microwave signal delivered by the oscillator. The circuit also has isolators to protect the low-noise microwave amplifier.

Fibers considered as through-port enable to obtain an optical spectrum using an optical spectrum analyzer. When there is no oscillation, working in open loop, through-port enables cavity ringdown characterization by sweeping a fast signal [15] and analyzes the detected signal, thanks to the oscilloscope. It can measure at the first optical output of the OEO by detection of an absorption peak. It enables to determine intrinsic and loaded  $Q$ -factor.  $MgF_2$  high- $Q$  resonator were fabricated and characterized at Femto-St Institute in Besançon. Best  $Q$ -factors determined by cavity ringdown are between  $10^9$  and  $10^{10}$  [16,17].

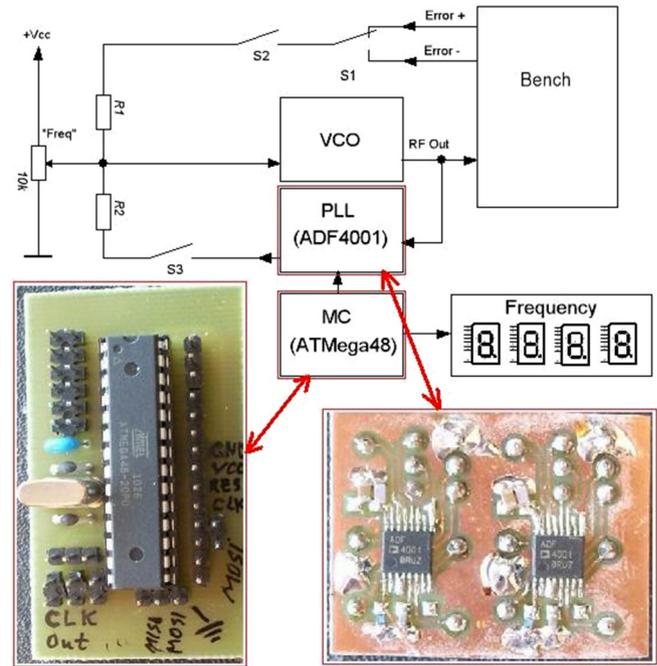
### 3 Stabilization of the laser

#### 3.1 Pound–Drever–Hall stabilization

Microwave signal generated by the OEO presents instabilities due to temperature. There is a need to lock the laser on this microwave signal to follow the resonance. The most efficient way is to develop a PDH stabilization: the PDH technique is a largely used and powerful approach for stabilizing the wavelength of light emitted by a laser [3,18]. The main principle of PDH technique is to give an electric feed back to a laser: at the resonance condition, transition of phase can be converted to an error reference and is fed back to control frequency of laser. This approach is known to be a reliable one in the time domain. This PDH is typically applied in a number of various lasers: the linewidth is then smaller than the resonance linewidth. A frequency control parameter is also available. To understand how PDH works, please refer to a previous work [19].

#### 3.2 Stabilization using acousto-optic cells

Principle of acousto-optic cells (AOC) is explained in references [20,21]. Choice of the range of frequency applied



**Fig. 3.** Principle of the generation of RF signals.

to the AOC is explained in reference [22]. The operation of the stabilized OEO consists in proceeding as follows: bulk acoustic waves are created from an error signal after the photodetector. Radio frequencies are between 55 and 65 MHz. A pair of quasi-identical cells provide the locking as required for the microwave signal detected after the photodiode. Concretely, with a  $Q$ -factor between  $2 \times 10^7$  and  $2 \times 10^{11}$ , the two radio frequencies vary from 2 kHz to 10 MHz. The 10 MHz maximum amplitude for those radio frequency signals should allow measuring resonators with relatively low  $Q$ -factor, especially better than  $2 \times 10^7$ . It would be difficult to work with resonators with  $Q$ -factors less than  $2 \times 10^7$  because as detailed in reference [22], our AOCs only allow a 10 MHz difference between the two used signals at 55 and 65 MHz in that case. On the contrary, an ultrahigh quality factor at  $10^{11}$  [14] requires a lower radio frequency difference of 2 kHz for driving the cells. AOCs are driven by two signals around 61 MHz. A synthesizer is used to change both frequencies. A numerically controlled oscillator is locked on a developed board for generating radio frequencies, as shown in Figure 3. The main advantage is the OEO stabilization. But there are potential limitations, such as difficulties when aligning two cells and inserting between laser and modulator.

### 4 Phase noise measurements setup

#### 4.1 Definitions

By definition, we can say that phase noise is like the power spectral density of the phase of one signal. Phase noise  $\varphi$  is given by

$$v(t) = A x \cos(2\pi f_0 t + \varphi(t)). \quad (6)$$

The definition of phase noise is

$$(f) = S\varphi(f)/2 \quad (7)$$

where  $S\varphi(f)$  is the one-sided spectral density of a phase shift of a signal, and  $f$  is the Fourier frequency. Despite  $S\varphi(f)$  being one-sided function, it is called the double-sideband spectral density of phase fluctuation. Phase noise can be defined as the PSD in a 1 Hz band at a certain offset from the carrier.

## 4.2 Realized system

A signal generated by a microwave synthesizer enables the validation of performances for phase noise system. Optoelectronic system has double delay lines. It operates with a 1.55  $\mu\text{m}$  wavelength laser. Cross-correlation enables a lower noise floor. To check validation of performances, comparison is performed between the phase noise datasheet of a commercial Anritsu synthesizer and the phase noise measured by the developed system. The noise floor of the system is then estimated. Noise floor of the instrument used for measuring is respectively determined as  $-170$  dBc/Hz at 10 kHz and  $-90$  dBc/Hz at 10 Hz from the 10 GHz carrier. Phase noise of the OEO is better than  $-125$  dBc/Hz at 10 kHz from the microwave carrier. Uncertainty budget is determined according to GUM (Guide of Uncertainty Measurements). The global uncertainty is  $\pm 2$  dB at  $2\sigma$  with accredited calibration [23,24]. Recent works concur with Integrated OEO [25] with good results with resonator on chip and athermal waveguides applied to ring resonators [26].

## 5 Conclusion

Experimental results on an optoelectronic oscillator with intensity modulator and a high- $Q$  minidisk resonator show that OEO based on a WGMR is relatively stable. It also shows that generated microwave signal presents a strong single peak in X-band. Phase noise of the realized OEO is better than  $-125$  dBc/Hz at 10 kHz from the microwave carrier. Perspectives should consist in setting up a more accurate laser lightwave coupling, increasing the WGMR's loaded  $Q$ -factor and test on other miniature optical coupling designs such as prisms. It should lead to the achievement of lower phase noise levels. A promising work is the investigation in on-chip micro-resonators. Laser stabilization with AOCs is still to be investigated, but the main effort is still made on classical PDH technique as it proves its capabilities. Experimental results for 2 km delay line with cross-correlation method show the capability of the developed system to measure phase noise of oscillators up to  $-90$  dBc/Hz at 10 Hz and  $-170$  dBc/Hz at 10 kHz from a carrier in X-band frequency range. Measurement uncertainty is  $\pm 2$  dB at  $2\sigma$  and depends on the repeatability of the measure, it is  $\pm 0.68$  dB at  $1\sigma$ .

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