

Home Search Collections Journals About Contact us My IOPscience

Polarization state and level repulsion in two-dimensional phononic crystals and waveguides in the presence of material anisotropy

This article has been downloaded from IOPscience. Please scroll down to see the full text article. 2010 J. Phys. D: Appl. Phys. 43 185401 (http://iopscience.iop.org/0022-3727/43/18/185401) View the table of contents for this issue, or go to the journal homepage for more

Download details: IP Address: 194.57.91.238 The article was downloaded on 22/04/2010 at 08:09

Please note that terms and conditions apply.

J. Phys. D: Appl. Phys. 43 (2010) 185401 (7pp)

Polarization state and level repulsion in two-dimensional phononic crystals and waveguides in the presence of material anisotropy

Younes Achaoui, Abdelkrim Khelif, Sarah Benchabane and Vincent Laude

Institut FEMTO-ST, Université de Franche-Comté, CNRS, ENSMM, UTBM; 32 avenue de l'Observatoire F-25044 Besançon, France

Received 30 November 2009, in final form 17 March 2010 Published 21 April 2010 Online at stacks.iop.org/JPhysD/43/185401

Abstract

We investigate the polarization of Bloch waves in two-dimensional piezoelectric phononic crystals and phononic crystal waveguides managed therein. It is found that in addition to the strong coupling induced for waves polarized in the plane of the periodic structuration, a weaker but non-negligible coupling of polarization components originates from material anisotropy. Numerical illustrations are given for an array of air holes in lithium niobate arranged according to a square lattice. It is observed that when a band mostly polarized in-plane gets close to a band mostly polarized out-of-plane, a phenomenon of repelling can occur, that in some instances introduces a local band gap. This interaction is accompanied by a transfer of the polarization state from one band to the other.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

Phononic crystals are periodic structures that can give rise to complete band gaps (BG) for acoustic waves in fluids or elastic waves (acoustic phonons) in solids [1, 2], in the very same way that photonic crystals prohibit the propagation of optical or electromagnetic waves [3, 4]. The dispersion of the bands constituting the band structure, the frequency position and the width of the band gaps are conditioned by the contrast between material constants of the constituent media on the one hand, and by the filling fraction, the geometrical shape of the inclusions and the lattice topology on the other hand. Within a frequency band gap, a phononic crystal acts as a mirror for incident waves, as a result of destructive interferences between waves scattered on the periodic inclusions. Thanks to the wide operating frequency range of acoustic and elastic waves, complete band gaps have been demonstrated theoretically and experimentally at different scales, for bulk waves [2, 5, 6]and surface waves [7-11], as well as for phononic crystal slabs [12–14]. Phononic crystals also allow for the obtaining of confined states or guided waves through the introduction of point or linear defects [15–18]. Phononic waveguides, resonators and stubs have been proposed as possible ways

to create filtering and multiplexing structures based on the coupling of resonance and waveguiding phenomena [19–21].

In the case of acoustic waves in fluids, because of the single polarization involved (longitudinal), the band structure in the perfect crystal case and the transmission coefficient in the waveguide case are usually considered sufficient to characterize a phononic crystal. But for elastic waves propagating in a solid, both transverse and longitudinal polarizations exist and are possibly coupled owing to the periodic structuration. Taking the polarization state into account in the analysis of band diagrams is hence compulsory to show a complete picture of elastic wave propagation. This has, for example, been shown by a previous study dedicated to polarization effects in a perfect 2D phononic crystal made of air inclusions in an epoxy matrix [22]. This work highlighted the influence of the filling fraction on the coupling between in-plane transverse and longitudinal polarizations, where in-plane refers to the plane normal to the inclusion axis. The in-plane polarization components were found to be more coupled for higher filling fractions, and a continuous variation of the polarization when the wavevector sweeps the first Brillouin zone was reported. This continuity of the elastic displacement fields along band structures has also been

investigated in order to study the repulsion level between different branches in the band diagram for both one- [23] or two- [24] dimensional phononic crystals. We are not aware of similar works for phononic crystals involving anisotropic materials or phononic waveguides, although the dependence of the guided waves dispersion on a change in the central inclusion radius or in the waveguide width has been reported recently [25, 26]. With the configurations proposed in these works, some branches initially located outside the band gap in the case of the perfect phononic crystal can enter or exit the band gap when the dimensions of the defect vary. The displacement field of some confined modes was reported as well and it was observed that following the same band as the Bloch wavevector varies in the first Brillouin zone, the polarization of the displacement field can change partially or totally. A detailed investigation of this phenomenon, however, remains to be performed.

In this paper, we first investigate the consequences of material anisotropy on the coupling of polarization components in two-dimensional phononic crystals. Of particular relevance is the combination of the effects of material anisotropy and of the periodic structuration. It is well known that a two-dimensional periodic structuration introduces a coupling for the in-plane polarization components, while the out-of-plane component remains decoupled. We here show that material anisotropy can result in the coupling of all polarization components. For illustration purposes, we numerically investigate the evolution of the polarization of Bloch waves in a two-dimensional piezoelectric phononic crystal composed of a square-lattice array of holes in lithium niobate (LiNbO₃). As a piezoelectric material, LiNbO₃ is anisotropic for elastic wave propagation, so that in general the two shear and the longitudinal components of the polarization are not decoupled. The coupling induced by the anisotropy of LiNbO₃ is rather weak compared with the coupling induced by the periodic structuration, but will be shown not to be negligible. In our analysis, we first concentrate on the perfectly periodic phononic crystal. The plane wave expansion (PWE) method combined with an energy balance criterion is used to compute band structures displaying additional information related to the weighting of each polarization. We underline cases where polarizations are exchanged between interacting bands or conversely when this exchange does not happen upon band crossing. The study is then extended to the case of a phononic waveguide obtained by inserting a line defect in the initial phononic crystal thanks to the super-cell technique.

2. Polarization coupling

In this section, we investigate the influence of the anisotropy on the coupling of polarization components in phononic crystals. The considered geometry and the definition of axes and Brillouin zone are given in figure 1. The following analysis as well as the computation of band structures and modal distributions in the next sections are based on the PWE method. The PWE method is based on a direct application of the Bloch– Floquet theorem to the representation of Bloch waves as the product of a periodic function, given by a discrete sum over



Figure 1. (*a*) 2D piezoelectric phononic crystal consisting of a two-dimensional square-lattice array of circular cylindrical holes in lithium niobate. (*b*) Corresponding first Brillouin zone.

Fourier harmonics in the reciprocal-lattice space, with a timeharmonic exponential function with frequency ω and Bloch wave vector k. For instance, the displacements in the x direction read

$$u_x(\mathbf{r}) = \left(\sum_{n=1}^N U_{xn} \exp(-\iota \mathbf{G}^n \mathbf{r}) \exp(-\iota \mathbf{k} \cdot \mathbf{r})\right), \quad (1)$$

where G^n are the reciprocal-lattice vectors and $\iota^2 = -1$. Similar expressions hold for u_y and u_z . We specifically use the formulation by Wilm *et al* for bulk and plate waves in piezoelectric media [27], which was later extended to surface waves in anisotropic and piezoelectric media [9, 10]. The representation of hollow inclusions follows the procedure exposed in [10]. The secular equation ((5) of [10]),

$$\omega^2 \tilde{R} \tilde{U} = \left(\sum_{i,j=1,3} \Gamma_i \tilde{A}_{ij} \Gamma_j \right) \tilde{U}, \qquad (2)$$

defines an eigenvalue problem for the frequency as a function of the wave vector and is used to obtain band structures. In this expression, \tilde{U} is a vector gathering the Fourier coefficients of the three displacements and the electric potential, and the matrices Γ_i , \tilde{A}_{ij} and \tilde{R} contain $4N \times 4N$ Fourier coefficients. The detailed expressions of the different matrices will be useful to investigate the incidence of anisotropy on Bloch waves and their polarization. These matrices read

$$\tilde{A}_{ij} = \begin{bmatrix} A_{ij0} & A_{ijG^1-G^2} & \dots & A_{ijG^1-G^N} \\ A_{ijG^2-G^1} & A_{ij0} & \dots & A_{ijG^2-G^N} \\ \vdots & \vdots & \ddots & \vdots \\ A_{ijG^N-G^1} & A_{ijG^N-G^2} & \dots & A_{ij0} \end{bmatrix},$$
(3)

$$\Gamma_{i} = \begin{bmatrix} (k_{i} + G_{i}^{1})I_{d} & & 0 \\ & (k_{i} + G_{i}^{2})I_{d} & & \\ & & \ddots & \\ 0 & & & (k_{i} + G_{i}^{N})I_{d} \end{bmatrix}, \quad (4)$$

$$\tilde{R} = \begin{bmatrix} \rho_{0}\tilde{I} & \rho_{G^{1}-G^{2}}\tilde{I} & \dots & \rho_{G^{1}-G^{N}}\tilde{I} \\ \rho_{G^{2}-G^{1}}\tilde{I} & \rho_{0}\tilde{I} & \dots & \rho_{G^{2}-G^{N}}\tilde{I} \\ \vdots & \vdots & \ddots & \vdots \\ \rho_{G^{N}-G^{1}}\tilde{I} & \rho_{G^{N}-G^{2}}\tilde{I} & \dots & \rho_{0}\tilde{I} \end{bmatrix},$$
(5)

Table 1. Shapes of the A_{ij} matrices in the case of materials with isotropic, cubic and trigonal 3m crystalline symmetry. Orientation along the principal crystallographic axes is assumed. Zero elements are indicated by dots (.) while non-zero values are indicated by circled crosses (\otimes).

Symmetry	A_{11G} or A_{22G}			A_{12G} or A_{21G}				$\tilde{A}_{G^m-G^n}$				
Isotropic or cubic (e.g. silicon)	$\begin{pmatrix} \otimes \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{pmatrix}$	⊗	⊗	⊗)	$\begin{pmatrix} \cdot \\ \otimes \\ \cdot \\ \cdot \end{pmatrix}$	⊗ • •		.)	$\begin{pmatrix} \otimes \\ \otimes \\ \cdot \\ \cdot \\ \cdot \end{pmatrix}$	⊗ ⊗	⊗	⊗)
Trigonal 3 <i>m</i> (e.g. lithium niobate)	$\begin{pmatrix} \otimes \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{pmatrix}$	⊗ ⊗	⊗ ⊗	$ \begin{pmatrix} \cdot \\ \otimes \\ \otimes \\ \otimes \end{pmatrix} $	$\begin{pmatrix} \cdot \\ \otimes \\ \otimes \\ \otimes \end{pmatrix}$	⊗ • •	⊗ • •	⊗	$\begin{pmatrix} \otimes \\ \otimes \\ \otimes \\ \otimes \\ \otimes \end{pmatrix}$	\otimes \otimes \otimes	\otimes \otimes \otimes	$\left(\begin{array}{c} \otimes \\ \otimes \\ \otimes \\ \otimes \end{array} \right)$

with $A_{ilG}(j, k) = c_{ijklG}$, $A_{ilG}(j, 4) = e_{lijG}$, $A_{ilG}(4, k) = e_{iklG}$, $A_{ilG}(4, 4) = -\epsilon_{ilG}$. I_d is the 4 × 4 identity matrix and $\tilde{I} = I_d$ but for $\tilde{I}(4, 4) = 0$. c_{ijkl} , e_{ijk} and ϵ_{ij} are the elastic, piezoelectric and dielectric tensors, respectively. The Γ_i and \tilde{R} matrices are each formed of $N^2 4 \times 4$ diagonal blocks. Material anisotropy enters the \tilde{A}_{ij} matrices are directly dependent on those of the material tensors c_{ijkl} , e_{ijk} and ϵ_{ij} . In turn, the influence of anisotropy in the secular equation (2) is contained in the matrix

$$\tilde{A} = \sum_{i,j=1,3} \Gamma_i \tilde{A}_{ij} \Gamma_j \tag{6}$$

appearing in the right-hand side. \tilde{A} retains the block structure of the \tilde{A}_{ij} matrices. More precisely, the (m, n)th sub-block reads

$$\tilde{A}_{G^m - G^n} = \sum_{i,j=1,3} (k_i + G_i^m) (k_j + G_j^n) A_{ijG^m - G^n}.$$
 (7)

The above expressions can be further detailed for a twodimensional phononic crystal. In this case, the summation i, j = 1, 2 and using the contracted notation for tensors we arrive at

$$A_{11G} = \begin{pmatrix} c_{11G} & c_{16G} & c_{15G} & e_{11G} \\ c_{61G} & c_{66G} & c_{65G} & e_{16G} \\ c_{51G} & c_{56G} & c_{55G} & e_{15G} \\ e_{11G} & e_{16G} & e_{15G} & -\epsilon_{11G} \end{pmatrix},$$

$$A_{12G} = \begin{pmatrix} c_{16G} & c_{12G} & c_{14G} & e_{21G} \\ c_{66G} & c_{62G} & c_{64G} & e_{26G} \\ c_{56G} & c_{52G} & c_{54G} & e_{25G} \\ e_{16G} & e_{12G} & e_{14G} & -\epsilon_{12G} \end{pmatrix},$$

$$A_{21G} = \begin{pmatrix} c_{61G} & c_{66G} & c_{65G} & e_{16G} \\ c_{21G} & c_{26G} & c_{25G} & e_{12G} \\ c_{41G} & c_{46G} & c_{45G} & e_{14G} \\ e_{21G} & e_{26G} & e_{25G} & -\epsilon_{21G} \end{pmatrix},$$

$$A_{22G} = \begin{pmatrix} c_{66G} & c_{62G} & c_{64G} & e_{26G} \\ c_{66G} & c_{62G} & c_{64G} & e_{26G} \\ c_{66G} & c_{42G} & c_{44G} & e_{24G} \\ e_{26G} & e_{22G} & e_{24G} & -\epsilon_{22G} \end{pmatrix}.$$

$$(8)$$

In the absence of any structuration, i.e. for a homogeneous material, the summations on the reciprocal-lattice vectors would be limited to G = 0, and the matrix \tilde{A} would be

formally equivalent to the Christoffel tensor [28]. In this case, propagation in the x direction would only involve the A_{110} matrix (respectively A_{220} for propagation in the y direction). The periodicity of the phononic crystal is manifested by nonzero G^m and G^n components for $(m, n) \neq 0$ and causes a mixing of matrix elements in equation (7), whatever the propagation direction k.

In the case of general anisotropic media, inspection of the block matrices in equation (8) reveals which polarization components are coupled. Such an analysis is straightforward but should be conducted for every crystallographic symmetry class and every material orientation considered. As an example, we have considered two cases in table 1. In the case of materials with isotropic or cubic crystalline symmetry (e.g. silicon), the periodic structuration results in non-zero off-diagonal terms coupling displacements u_x and u_y , but the out-of-plane displacement u_7 and the electric potential ϕ are uncoupled. This directly explains the coupling between in-plane polarization components and the decoupling of the out-of-plane polarization component in isotropic 2D phononic crystals. The case of materials with trigonal 3m symmetry (e.g. lithium niobate) is different. In the homogeneous material, propagation along the x and y directions occurs according either to a non-piezoelectrically coupled wave (decoupled u_x polarization) or to piezoelectrically coupled waves (coupled u_{y} , u_{z} and ϕ polarization). With the additional consideration of a periodic structuration in the (x, y) plane, all polarization components get coupled. This analysis, of course, is based only on the nullity or not of matrix elements, and the strength of the coupling induced by the periodic structuration and material anisotropy depends quantitatively on the actual magnitude of the matrix elements. Numerical illustrations are given in the subsequent sections in the case of lithium niobate.

3. Two-dimensional piezoelectric phononic crystal

We consider in the following a two-dimensional piezoelectric phononic crystal made of a square-lattice array of circular cylindrical holes in LiNbO₃. The crystallographic orientation of LiNbO₃ is chosen to be the Z-cut, so that the Z crystallographic axis is parallel to the z-axis of the reference frame of figure 1(a). The filling fraction is 64%. Theoretical and experimental properties of such a phononic crystal have been investigated before, and the existence of a complete band gap for both bulk and surface waves has been demonstrated [10, 11, 29]. Here we further consider the evolution of the polarization of Bloch waves.

The two-dimensional Fourier expansions are truncated to the 36 first harmonics in this section, as a result of a compromise between convergence and computation time, but also to obtain band structures that are directly comparable to those obtained for waveguides with the super-cell technique in the next section. With this choice, convergence in terms of frequencies is within a few per cent of the high number of harmonics limit.

In order to avoid possible confusions, we use throughout this paper the displacement field components u_x , u_y and u_z to represent polarizations. In this way, we avoid using the terminology of longitudinal, horizontal and vertical shear polarizations, which are dependent on the direction of propagation. In the band structures, polarization is represented by three positive numbers summing to unity. For instance, the amount of polarization along the x direction is given by

$$p_x^2 = \frac{\int |u_x|^2 \mathrm{d}\mathbf{r}}{\int (|u_x|^2 + |u_y|^2 + |u_z|^2) \,\mathrm{d}\mathbf{r}},\tag{9}$$

with the integral taken over the unit-cell. Similar expressions hold for the amounts of polarization p_y^2 and p_z^2 measured along the *y*- and the *z*-axes, respectively.

Figure 2 displays the band structure giving the dispersion relation for elastic waves propagating in the phononic crystal of figure 1(*a*). The structure shows a complete band gap with a 33% fractional bandwidth. The three band structures actually display the same $\omega(k)$ dispersion relations, but with the additional information of the amounts of polarization p_x^2 , p_y^2 and p_z^2 in figures 2(*a*), (*b*) and (*c*), respectively.

It can be observed in figure 2 that the bands do not in general possess a pure polarization, except for some portions of them. The coupling of the in-plane polarization components $(u_x \text{ and } u_y)$, however, appears much stronger than the coupling with the out-of-plane component (u_z) , especially above the complete band gap. This observation is fully consistent with the results of the previous section. If it were not for the anisotropy of LiNbO₃, the two-dimensional periodic structuration would introduce a strong coupling of the in-plane polarization components, but the out-of-plane component would remain completely decoupled. The coupling between in-plane polarization components is especially strong in figure 2 for propagation directions that encompass the M point of the first Brillouin zone. The comparatively weaker coupling of all three polarization components is caused by material anisotropy.

As a general rule, it can be observed that the polarization varies continuously as the Bloch wave vector sweeps the first Brillouin zone. There are, however, intriguing points in the band structure where bands cross without interacting or conversely interact and repel each other. Points at which repelling between bands occurs have been labelled A to G in figure 2. Figure 3 displays closer views at these seven points, with the colour indicating the p_z^2 component of the polarization. Each couple of repelling bands is composed



Figure 2. Band structure of the phononic crystal depicted in figure 1(*a*). The complete band gap is indicated by the greyed region. The three band structures depict the same dispersion relations but the colouring of the bands shows the amount of polarization along (*a*) the *x*-axis, (*b*) the *y*-axis and (*c*) the *z*-axis. Points A, B, C, D, E, F and G mark the (k, ω) positions of the first seven intersections of repelling branches.

of a mostly in-plane polarized band and of a mostly outof-plane polarized band, which leads us to the conclusion that repelling occurs as a result of the coupling provided by the anisotropy of LiNbO₃. It can be observed that when bands repel, they exchange their polarization state, so that the polarization remains a continuous function of the wave vector k.

Two different cases are further observed. Repelling at points C, D, F and G introduces a local band gap, while, conversely, repelling at points A, B and E does not introduce any. We observe that the occurrence of a local band gap



Figure 3. Enlarged dispersion relations in figure 2(c) in the vicinity of repelling bands near (*a*) point A, (*b*) point B, (*c*) point C and D, (*d*) point E, (*e*) point F and (*f*) point G.

is conditioned by the two repelling bands being either on opposite sides of a horizontal line passing at the repelling point (presence of a local BG) or on the same side (absence of a local BG).

Figure 4 illustrates in more detail how the polarization is transferred between the two repelling bands at point C. At the left of point C, the upper band is mostly polarized along z, while the lower band is mostly polarized in-plane and rather along the *y*-axis. After repelling, the respective polarizations have been exchanged from out-of-plane to in-plane, and vice versa.

4. Piezoelectric phononic crystal waveguide

In this section, we consider a phononic crystal waveguide managed by removing a row of holes from the phononic crystal along the x direction and investigate how the polarization and repelling properties obtained in the previous section for the perfectly periodic phononic crystal are modified. The PWE method can be used to obtain the dispersion of guided waves for frequencies that fall within the complete band gap, using the super-cell technique [25, 26]. In practice, the considered unit-cell shown in figure 5 is made 7 times longer along the y direction, as compared with the unit-cell in figure 2, and thus includes three holes on both sides



Figure 4. Spatial distribution of the polarization components u_x , u_y and u_z of the displacement field for points before and after the repulsion in point C.

of the central guiding section. The holes have the same filling fraction as in the previous section and the number of Fourier harmonics has been increased by a factor of 6 in the y direction to achieve convergence conditions similar to those obtained in the previous section. Because of periodicity in the computations, six holes separate neighbouring waveguides.



Figure 5. Phononic crystal waveguide created by removing a row of holes from the phononic crystal along the x direction. The framed box shows the unit-cell used for super-cell computations.

We have checked that this separation is actually sufficient to isolate the periodically repeated waveguides by computing the band structure along the Γ Y direction of the first Brillouin zone and verifying that only flat bands are obtained within the complete band gap (if we had obtained dispersion then this would have been an indication of coupling between adjacent waveguides).

Figure 6 displays the dispersion relations of Bloch waves guided by the structure in figure 5 and propagating along the x direction for frequencies within the complete phononic band gap. As for the band structure of the perfectly periodic phononic crystal depicted in figure 2, the band structure for guided Bloch waves is repeated three times with the additional information of the amounts of polarization p_x^2 , p_y^2 , and p_z^2 in figures 6(a), (b) and (c), respectively. Eight different bands are apparent and are numbered sequentially. Bands 1 and 4 are mostly polarized in-plane and repel midways between the Γ and the X points. Bands 2 and 6 are also mostly polarized in-plane. For all these bands, the distribution between in-plane components p_x and p_y does not remain constant as the wavevector varies from the Γ to the X points. Band 3 is purely polarized out-of-plane (vertical shear wave), while band 8 is mostly polarized out-of-plane. The cases of bands 5 and 7 are more intriguing, since these two bands are, respectively, mostly polarized in-plane and out-of-plane before points I and J where they repel, create a local band gap and abruptly exchange their polarization state. The mechanism for the coupling between these two bands is made possible thanks to the anisotropy of LiNbO₃, similarly to what was discussed in section 2.

Figure 7 illustrates how polarization transfer occurs at the repelling of bands 5 and 7. We have chosen to show the modulus of the real part of the displacements u_x . It can be observed that the distribution of u_x at point K on band 7 is transferred without almost any alteration to point J on band 5. At the wavevector for which the bands are the closest, i.e. at points I and L, the modal distributions are very similar. In



Figure 6. Band structure along the ΓX direction for the phononic waveguide displayed in figure 5, showing the dispersion relation for guided Bloch waves. The band structure is repeated three times with the information of the amount of polarization (*a*) p_x^2 , (*b*) p_y^2 and (*c*) p_z^2 .

the absence of anisotropy, the repelling point would have been replaced by a crossing of the two bands, and points H and M would have been on the same band (similarly, points J and K would have been on the same band).

5. Conclusion

In summary, we have investigated the polarization of Bloch waves in a two-dimensional piezoelectric phononic crystal and a phononic crystal waveguide managed inside it. By examining the structure of the matrices involved in the secular equation and by studying band structures, it was found that in addition to the strong coupling induced for waves polarized in the plane of the periodic structuration, a weaker but nonnegligible coupling of all polarization components originates from material anisotropy. As a consequence, when a band



Figure 7. Spatial distribution of the modulus of the real part of the displacements u_x at the repelling of bands 5 and 7, shown for the six points H to M indicated in figure 6. Points H, I and J are placed along band 5 before, at and after the repelling point, respectively. Points K, L and M are similarly placed along band 7.

mostly polarized in-plane gets close to a band mostly polarized out-of-plane, a phenomenon of repelling can occur between them that in some instances introduces a local band gap. This interaction is accompanied by a transfer of the polarization state from one band to the other. The findings in this paper illustrate that when anisotropic materials are involved, dispersion relations for Bloch waves in phononic crystals in the form $\omega(k)$ do not give a complete picture of wave propagation and must be supplemented with the dependence of the polarization on the wavevector.

References

- Sigalas M and Economou E N 1993 Band structure of elastic waves in two dimensional systems *Solid State Commun.* 86 141
- [2] Kushwaha M S, Halevi P, Dobrzynski L and Djafari-Rouhani B 1993 Acoustic band structure of periodic elastic composites *Phys. Rev. Lett.* **71** 2022
- [3] Yablonovitch E 1987 Inhibited spontaneous emission in solid-state physics and electronics *Phys. Rev. Lett.* 58 2059
- [4] John S 1987 Strong localization of photons in certain disordered dielectric superlattices *Phys. Rev. Lett.* 58 2486
- [5] Kushwaha M S, Halevi P, Martinez G, Dobrzynski L and Djafari-Rouhani B 1994 Theory of acoustic band structure of periodic elastic composites *Phys. Rev.* B 49 2313
- [6] Kushwaha M S and Halevi P 1994 Band-gap engineering in periodic elastic composites *Appl. Phys. Lett.* 64 1085
- [7] Tanaka Y and Tamura S I 1998 Surface acoustic waves in two-dimensional periodic elastic structures *Phys. Rev.* B 58 7958
- [8] Tanaka Y and Tamura S I 1999 Acoustic stop bands of surface and bulk modes in two-dimensional phononic lattices consisting of aluminum and a polymer *Phys. Rev. B* 60 13294

- [9] Wu T-T, Huang Z G and Lin S 2004 Surface and bulk acoustic waves in two-dimensional phononic crystal consisting of materials with general anisotropy *Phys. Rev. B* 69 094301
- [10] Laude V, Wilm M, Benchabane S and Khelif A 2005 Full band gap for surface acoustic waves in a piezoelectric phononic crystal *Phys. Rev.* E **71** 036607
- [11] Benchabane S, Khelif A, Rauch J-Y, Robert L and Laude V 2006 Evidence for complete surface wave band gap in a piezoelectric phononic crystal *Phys. Rev.* E 73 065601(R)
- [12] Khelif A, Aoubiza B, Mohammadi S, Adibi A and Laude V 2006 Complete band gaps in two-dimensional phononic crystal slabs *Phys. Rev.* E 74 046610
- [13] Hsu J C and Wu T-T 2006 Efficient formulation for band-structure calculations of two-dimensional phonic-crystal plates *Phys. Rev.* B 74 144303
- [14] Charles C, Bonello B and Ganot F 2006 Propagation of guided elastic waves in 2D phononic crystals *Ultrasonics* 44 1209(E)
- [15] Sigalas M M 1998 Defect states of acoustic waves in a two-dimensional lattice of solid cylinders J. Appl. Phys. 84 3026
- [16] Torres M, Montero de Espinosa F R, García-Pablos D and García N 1999 Sonic band gaps in finite elastic media: Surface states and localization phenomena in linear and point defects *Phys. Rev. Lett.* 82 3054
- [17] Kafesaki M, Sigalas M M and García N 2000 Frequency modulation in the transmittivity of wave guides in elastic-wave band-gap materials *Phys. Rev. Lett.* 85 4044
- [18] Chandra H, Deymier P A and Vasseur J O 2004 Elastic wave propagation along waveguides in three-dimensional phononic crystals *Phys. Rev.* B 70 054302
- [19] Khelif A, Choujaa A, Djafari-Rouhani B, Wilm M, Ballandras S and Laude V 2003 Trapping and guiding of acoustic waves by defect modes in a full-band-gap ultrasonic crystal *Phys. Rev.* B 68 214301
- [20] Pennec Y, Djafari-Rouhani B, Vasseur J O, Larabi A, Khelif H, Choujaa A, Benchabane S and Laude V 2005 Acoustic channel drop tunneling in a phononic crystal *Appl. Phys. Lett.* 87 261912
- [21] Sun J H and Wu T-T 2005 Analyses of mode coupling in joined parallel phononic crystal waveguides *Phys. Rev.* B 71 174303
- [22] Manzanares-Martinez B and Ramos-Mendieta F 2007 Sagittal acoustic waves in phononic crystals: k-dependent polarization Phys. Rev. B 76 134303
- [23] Kato H, Maris H J and Tamura S I 1996 Resonant-mode conversion and transmission of phonons in superlattices *Phys. Rev. B* 53 7884
- [24] Wu T-T and Huang Z-G 2004 Level repulsions of bulk acoustic waves in composite materials *Phys. Rev. B* 70 214304
- [25] Sun J H and Wu T T 2007 Propagation of acoustic waves in phononic crystal plates and waveguides using a finite difference time domain method *Phys. Rev.* B 76 104304
- [26] Vasseur J O, Deymier P A, Djafari-Rouhani B, Pennec Y and Hladky-Hennion A-C 2008 Absolute forbidden bands and waveguiding in two-dimensional phononic crystal plates *Phys. Rev.* B 77 085415
- [27] Wilm M, Ballandras S, Laude V and Pastureaud T 2002 A full 3D plane wave expansion model for 1–3 piezoelectric composite structures J. Acoust. Soc. Am. 112 943
- [28] Royer D and Dieulesaint E 1999 Ondes Élastiques Dans les Solides vol 1 (Paris: Masson)
- [29] Kokkonen K, Kaivola M, Benchabane S, Khelif A and Laude V 2007 Scattering of surface acoustic waves by a phononic crystal revealed by heterodyne interferometry *Appl. Phys. Lett.* **91** 083517